

RFI Detection and Mitigation for Advanced Correlators in Interferometric Radiometers

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Abstract: This work presents the first RFI detection and mitigation algorithm for interferometric radiometers that will be implemented in the correlator unit. The algorithm operates in the time and frequency domains, applying polarimetric and statistical tests in both domains, exhibiting a tunable and arbitrary low probability of false alarm. It is scalable to an arbitrary number of receivers, and it is optimized in terms of quantization bits and implementation of the cross-correlations in the time or frequency domains for hardware resources saving. New features of this algorithm are the computation of the Stokes parameters per frequency bin in the Short-Time Fourier Transform, and a new parameter called Polarimetric Kurtosis. If RFI is detected in one domain or in both, it is removed using the calculated blanking masks. Optimum algorithm parameters are computed, such as length of the FFTs, threshold selection for a given probability of false alarm, and selection of the blanking masks. Last, an important result refers to the application of the Parseval's Theorem for the computation of the cross-correlations in the frequency domain, instead of in the time domain, which is more efficient, and leads to smaller errors even using moderate quantization levels. The algorithm has been developed in the framework of ESA's technology preparation for a potential L-band radiometer mission beyond SMOS. However, it is also applicable to (polarimetric) real aperture radiometers, and its performance improves if more than one bit is used in the signal quantization.

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1. Introduction

Radio-Frequency Interference (RFI) signals are undesired electromagnetic emissions that can degrade the performance of any receiver. Nowadays, the concern about the RFI phenomenon is increasing due to the high number of RFI occurrences detected, and this problem is expected to grow even more in the future because of the pervasive use and abuse of wireless technologies around the world. RFI signals are either those illegally emitted at bands reserved for passive observations (in-band effect), or those that are legally emitted in adjacent bands, but a fraction of their power leaks into the bandwidth of the radiometer (near-band effect), or even an harmonic emission at a much lower frequency band. The origin of these RFI signals can be of very different nature: they can be lower harmonics, inter-modulation products, out-of-band emissions, or even intentional emissions designed to override a particular frequency band. According to [1], the

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allocated bands provide a statutory protection, with no guarantee against interference occurrences from accidental out-of-band emissions or intentional jamming. Therefore, RFI has become a dangerous threat for passive remote sensing and, in particular, for Microwave Radiometry (MWR), as microwave radiometers have high sensitivity requirements, of the order of a Kelvin, or less. *→reference?*

In [2] a comprehensive literature review on RFI detection and mitigation (D/M) techniques in Earth Observation by means of passive microwave (i.e., radiometry and GNSS-R) is presented. Existing D/M techniques can be classified as parametric (designed to mitigate a particular type RFI signal, e.g., a CW signal), or non-parametric (RFI-type agnostic). These techniques can also be classified according to their domain of operation: time domain, frequency domain, statistical domain, polarimetry domain, or space domain (e.g., direction of arrival followed by beamforming or null-steering antennas). The performance of each technique is highly dependent on the RFI scenario, and RFI D/M algorithms may combine techniques from several domains to be more effective [3], e.g. time-statistical domains [4], time-frequency domains [5], frequency-statistical domains [6], time-scale domains and Wavelet Packet Decomposition (WPD) [7], signal sub-spaces decomposition (Karhunen-Loève Transform or KLT [8], Principal Component Analysis or PCA [9], Independent Component Analysis or ICA [10], multi-lag correlations [11], and time-space domains (e.g. adaptive beamforming / null-steering) [12, 13].

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There are two types of microwave radiometers: real and synthetic aperture ones, and they can be single or dual polarization, or fully polarimetric if they measure the full Stokes vector [14]. Real aperture radiometers have a single antenna whose beam(s) determines the spatial resolution, and the image is formed by scanning the beam(s). Synthetic aperture radiometers have multiple small antennas, and the complex cross-correlation of the signals collected by each pair of antennas provides a sample of the so-called “visibility function”, which corresponds to a spectral component of the apparent brightness temperature. The image is then formed by Fourier synthesis techniques.

In synthetic aperture radiometers, a cooperative RFI detection approach may be taken into account, assuming that the same RFI signal will likely be collected by all antenna elements, as they are physically close. However, although cooperative RFI mitigation may be applied in the simplest time, frequency, and statistical domain algorithms, it is not feasible in other approaches, or in a multi-domain approach. The analysis of RFI in synthetic aperture radiometers was first studied in [15], and found that it could be very severe. Therefore, the RFI mitigation must be applied to the signals received from each single antenna element before they are cross-correlated. It is important to note that the dynamic range of the RFI signals that can be mitigated is strongly related to the number of bits used in the quantization process, and the use (or not) of an Automatic Gain Control (AGC) stage. For example, if the number of bits is low and there is a strong RFI, the noise signal to be correlated will be totally masked by the RFI, and either the correlation is that of the RFI signal, or –if cleaned– the cross-correlation will be zero, as the noise signal is under the quantization noise. Moreover, the performance of RFI mitigation techniques after correlation is limited, as some of such filtering techniques only allow the removal of abnormally high brightness temperature spots with accurate geo-localization of the RFI source (e.g. [12, 16, 17]).

In this study, an RFI detection and mitigation algorithm is presented as part of the technology developments towards an SMOS follow-on mission. The algorithm has been conceived to operate on 1-bit quantized signals only, as provided by the receivers connected to each dual-polarization antenna in the interferometric array, but it can also be implemented if softer (i.e., with more bits) quantization schemes are used. The 1-bit quantization is the one that produces the strongest clipping of the amplitude signal and the largest spectrum spread, and it affects the signal auto-correlation, the cross-correlation of two 1-bit quantized signals, the Fourier transform of the cross-correlation function, and the variance of the measurements (i.e., effective integration time smaller than the integration time) [18, 19]. Since the amplitude information is lost, the instantaneous power

information is also lost. Even though the 1-bit quantization makes the RFI mitigation task more difficult and less performant, some alternatives can be applied. In particular, two new RFI mitigation approaches are proposed in this study: the calculation of the Stokes parameters per frequency bin in the Short-Time Fourier Transform (STFT), and the Polarimetric Kurtosis, which are explained in the next section.

2. Materials and Methods

The proposed inputs for the new RFI detection and mitigation algorithm correspond to the outputs of the new receivers conceived for the SMOS follow-on mission. These include:

- X_{In} , X_{Qn} , Y_{In} , Y_{Qn} : four 1-bit data streams per receiver element n (from $n = 1 \dots N_{receivers}$) at 57.69375 MHz, being X/Y the polarization, and I/Q the in-phase/quadrature components,
- X_{Pn} , Y_{Pn} : two multi-bit Power Measurement System (PMS) streams per receiver element n (from $n = 1 \dots N_{receivers}$), and per polarization at ~ 28 kS/s.

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The proposed algorithm is fully tunable, even while in orbit, and some configurable parameters are:

- N is the number of samples per integration period. In this study $N = 11,538,432$ corresponding to an integration time of ~ 200 ms at the clock sampling frequency.
- K is the number of points of the Fourier transform, or number of points in the spectrum. K is an optimization parameter, but it can be reduced to a smaller power-of-two number if needed, during the implementation phase for FPGA resource utilization optimization.
- M is the number of time segments of the STFT in which the signal is divided. It is defined as $M = \gamma \cdot N / K$, where γ is the windowing factor. As it will be shown in the next section, $\gamma = 2$ which is the minimum windowing factor necessary to apply a non-rectangular window function.
- R_{tot} is the total number of receivers of the system.
- R_{avg} is the number of receivers that are averaged in the RFI detection process. It will be assumed that $R_{avg} = R_{tot}$. In the case of a real aperture radiometer $R_{avg} = R_{tot} = 1$.
- α_{th} is the detection threshold for statistical and polarimetry metrics to determine if an RFI signal is present or not, and it controls the probability of detection and the probability of false alarm. The parameter α_{th} may take three different specific values: α_{th}^{time} for temporal moments, α_{th}^{freq} for spectral moments, and α_{th}^{all} for all-signal moments.
- β_{th} is the maximum blanking threshold. The RFI mitigation is based on the excision of the contaminated samples out of the set of all transformed samples. The RFI mitigation operates efficiently if a reduced number of samples contain the largest fraction of the RFI power.

2.1. RFI Detection and Mitigation Algorithm Description

Figure 1 shows the overall block diagram of the proposed RFI mitigation algorithm. After an initial **windowing** to reduce the Gibbs effect associated to the truncation of the data streams, the signal spectrum is computed (**FFT**). **Calibration** measurements are acquired in RFI-free conditions, and allow to infer the receiver's chain frequency response, which will have to be compensated in subsequent measurements. **Equalization** is performed during normal acquisitions, that may or may not be affected by RFI, to compensate for the receiver's frequency response. Once the incoming signal's spectrum has been whitened (i.e., "flattened" to look like Additive White Gaussian Noise -AWGN- in RFI-free conditions), **statistical** and **polarimetric tests** are applied both in the **time or frequency** domains to detect the presence of RFI. When RFI is detected in one of these domains using any of the techniques, a **blanking mask** is calculated for either the **time or frequency domains**.

The outputs of this RFI mitigation algorithm contain both final and intermediate products, in the form of the averaged unmitigated and mitigated PMS measurements, and the computed blanking masks that will be used to mitigate the RFI prior to the correlator.

In the following subsections each of the blocks are described.

2.1.1. Windowing

Resolution in the temporal domain σ_t , and in the frequency domain σ_f are related, and constrained by the so-called Gabor limit [20].

$$\sigma_t \cdot \sigma_f \geq \frac{1}{4\pi}, \quad (1)$$

The selection of the window coefficients determines the amount of spectral leakage in the Fourier transform output. The Square Root Hamming window function (equation 2) has been selected for this application, because it provides a good trade-off between frequency resolution and side-lobe rejection, and it can fulfill the squared perfect reconstruction condition of equation 3. The window function is defined as:

$$w[k] = \sqrt{\frac{1}{2} \left[1 - \frac{1-\beta}{\beta} \cos\left(\frac{2\pi k}{K}\right) \right]}, \beta = \frac{25}{46}, 0 \leq k < K, \quad (2)$$

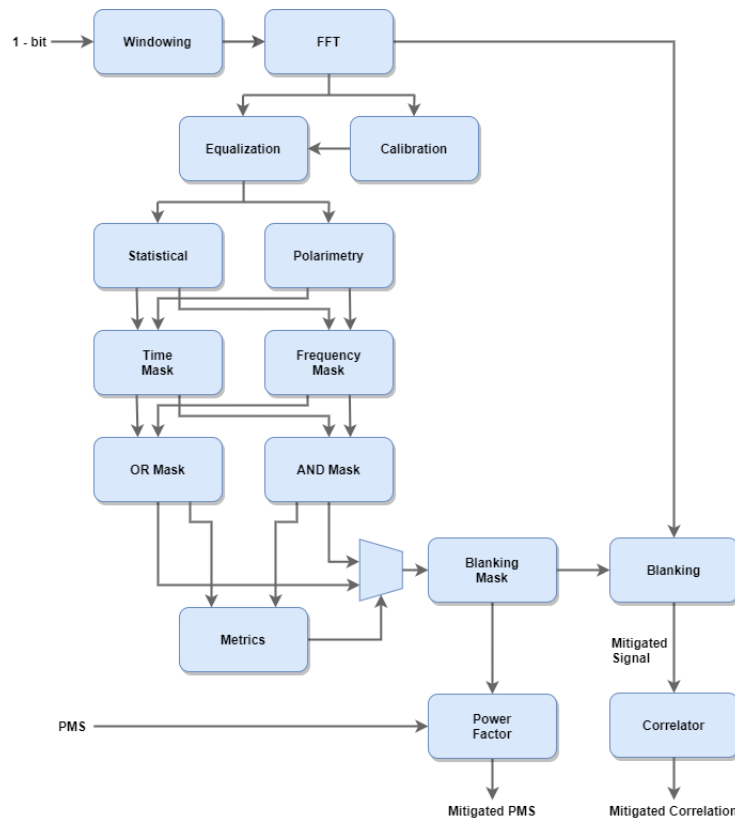


Figure 1. Overall block diagram of the RFI mitigation proposed algorithm.

In order to reconstruct the signal properly, the signal has to be windowed at least every $K/2$ samples. This turns the windowing factor γ , mentioned in the previous section, equal to 2. Setting this value larger than 2 may be helpful for the signal reconstruction in some cases, at the expense of increasing the required computational resources. However, the Square Root Hamming window function fulfills the following condition:

$$w^2[k] + w^2\left[k - \frac{K}{2}\right] = 1, \quad (3)$$

and therefore, windowing the input signal every $K/2$ samples is enough to reconstruct the signal back to the time domain.

2.1.2. Spectral Computation

The Short-Time Fourier Transform (STFT) is the most used technique for RFI excision. The signal is filtered in the time-frequency space in order to remove the RFI components before being transformed back to the time-domain (Figure 2, left).

2.1.3. Calibration and Equalization

Calibration and equalization are two stages needed to compensate for the effects of the non-flat frequency response of the receiver when applying some of the RFI mitigation techniques considered in this algorithm, such as cross-spectrum Kurtosis or Polarimetry. The calibration frequency responses $Z_r^{cal}[k]$, with $Z = X$ or Y , and r being the receiver number, are calculated as:

$$Z_r^{cal}[k] = \sqrt{\frac{1}{M} \sum_{m=0}^{M-1} |Z_r[m, k]|^2}, \quad (4)$$

where M is the number of STFT being averaged, and the equalized frequency responses $Z_r^{eq}[k]$, as:

$$Z_r^{eq}[m, k] = \frac{Z_r[m, k]}{Z_r^{cal}[k]}. \quad (5)$$

Note that the normalization is performed in the complex values instead of power in order to keep the power balance among different polarizations and receivers. Note also that the spectral calibration is particular for each receiver and polarization, as receiving channels are different. Calibration and equalization results are illustrated graphically in Figure 2, right, for a sample receiver.

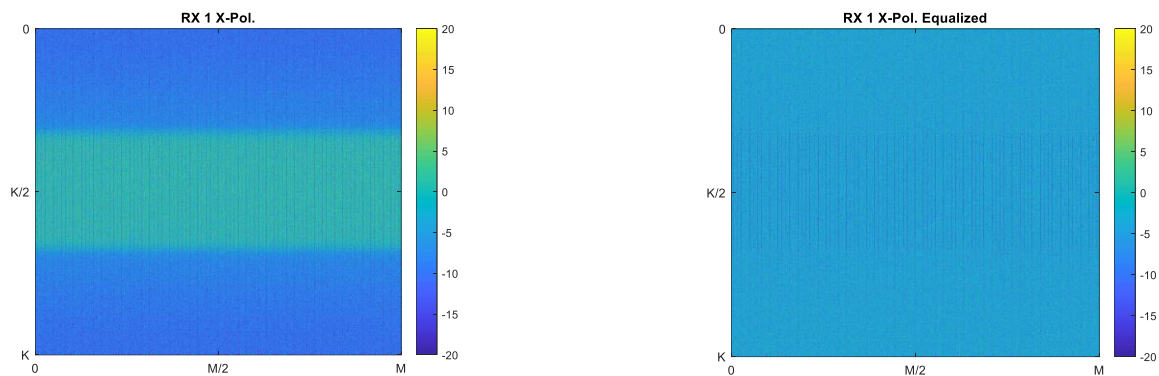


Figure 2. Modulus square of the STFT of the X-pol. at a sample receiver (a) before, and (b) after equalization. The vertical lines appearing in both figures are due to the clipping of the input receiver signal due to the strong RFI signal.

Time and frequency decomposition, calibration and equalization must be performed for each received signal. However, under some assumptions, like that the RFI pulses are received in the same samples at each receiver (determined by the array size and the off-boresight direction of arrival), or that the frequencies or frequency band of RFI signals at each receiver are equal, the number of STFT to be performed may be reduced, even up to 1 in the most extreme case.

2.1.4. Statistic and Polarimetry Tests

The proposed RFI detection algorithm is based on the calculation of some statistical and polarimetric moments over the aggregated time-frequency bins of the different receivers of the system.

- Stokes Parameters

The definition of the modified Stokes parameters for microwave radiometry can be combined with the multi-receiver approach, obtaining an averaged squared Stokes vector $S'[m, k]$ per each bin of the STFT as:

$$S'[m, k] = \begin{bmatrix} s_1^2[m, k] \\ s_2^2[m, k] \\ s_3^2[m, k] \\ s_4^2[m, k] \end{bmatrix} = \frac{1}{R_{avg}} \sum_{r=1}^{R_{avg}} \begin{bmatrix} |X_r^{eq}[m, k]|^4 \\ |Y_r^{eq}[m, k]|^4 \\ 4(\text{Re}\{X_r^{eq}[m, k] \cdot (Y_r^{eq}[m, k])^*\})^2 \\ 4(\text{Im}\{X_r^{eq}[m, k] \cdot (Y_r^{eq}[m, k])^*\})^2 \end{bmatrix}, \quad (6)$$

where $[m, k]$ are the time and frequency indices of the bin under evaluation, (s_1, s_2, s_3, s_4) are the first, second, third, and fourth multi-receiver squared Stokes parameters respectively, and R_{avg} is the number of receivers whose outputs are averaged.

- Kurtosis and Polarimetric Kurtosis

Kurtosis is the best statistical-based RFI detection algorithm for almost all kinds of interfering signals, although it is known that it has a blind spot for sinusoidal and chirp interfering signals of 50% duty cycle [21]. When combined with the Fourier transform, it is usually called Spectral Kurtosis, since the statistical test is applied per frequency bin. It can be mathematically computed as the ratio between the fourth central moment of a random variable and the square of its variance (second central moment). However, in practice, since thermal noise is zero-mean, and hardware has a calibrated DC offset, non-central moments are equivalent and used for the calculation of the Kurtosis.

At this time, the new “Polarimetric Kurtosis” observable can be introduced as:

$$\begin{bmatrix} k_1^{all} \\ k_2^{all} \\ k_3^{all} \\ k_4^{all} \end{bmatrix} = \frac{1}{M} \cdot \frac{1}{K} \sum_{m=0}^{M-1} \sum_{k=0}^{K-1} \begin{bmatrix} s_1^2[m, k]/(p_1^{all})^2 \\ s_2^2[m, k]/(p_2^{all})^2 \\ s_3^2[m, k]/(p_1^{all} \cdot p_2^{all}) \\ s_4^2[m, k]/(p_1^{all} \cdot p_2^{all}) \end{bmatrix}, \quad (7)$$

where:

$$p_{1,2}^{all} = \frac{1}{R_{avg}} \cdot \frac{1}{M} \cdot \frac{1}{K} \sum_{r=1}^{R_{avg}} \sum_{m=0}^{M-1} \sum_{k=0}^{K-1} s_{1,2}^2 r[m, k], \quad (8)$$

the first and second components ($k_{1,2}^{all}$) are the conventional complex sample Kurtosis for the X and Y polarization respectively, and the third and fourth components ($k_{3,4}^{all}$) are obtained as the ratio between the square of the third and fourth multi-receiver Stokes parameters, and the product of the second moments at X and Y polarizations (eqn. (8)). Note that eqn. (7) expresses the Polarimetric Kurtosis parameters for the bins within the integration time in both domains.

- Time-frequency Moments

Once the Polarimetric Kurtosis parameters are defined for “all” bins, it is straightforward to define the same metrics along the time and frequency domains. Instead of averaging all the bins of the STFT together, the integration may be done only in one of the STFT matrix dimensions, either time or frequency.

If the averaging is performed across the cross-frequency bins, the result can be named as Temporal Polarimetric Kurtosis:

$$\begin{bmatrix} k_1^{time}[m] \\ k_2^{time}[m] \\ k_3^{time}[m] \\ k_4^{time}[m] \end{bmatrix} = \frac{1}{K} \sum_{k=0}^{K-1} \begin{bmatrix} s_1^2[m, k]/(p_1^{time}[m])^2 \\ s_2^2[m, k]/(p_2^{time}[m])^2 \\ s_3^2[m, k]/(p_1^{time}[m] \cdot p_2^{time}[m]) \\ s_4^2[m, k]/(p_1^{time}[m] \cdot p_2^{time}[m]) \end{bmatrix}, \quad (9)$$

where:

$$p_{1,2}^{time}[m] = \frac{1}{R_{avg}} \cdot \frac{1}{K} \sum_{r=1}^{R_{avg}} \sum_{k=0}^{K-1} s_{1,2,r}^2[m, k]. \quad (10)$$

If the averaging is performed across the temporal bins, the result can be named as Spectral Polarimetric Kurtosis:

$$\begin{bmatrix} k_1^{freq}[k] \\ k_2^{freq}[k] \\ k_3^{freq}[k] \\ k_4^{freq}[k] \end{bmatrix} = \frac{1}{M} \sum_{m=0}^{M-1} \begin{bmatrix} s_1^2[m, k] / (p_1^{freq}[k])^2 \\ s_2^2[m, k] / (p_2^{freq}[k])^2 \\ s_3^2[m, k] / (p_1^{freq}[k] \cdot p_2^{freq}[k]) \\ s_4^2[m, k] / (p_1^{freq}[k] \cdot p_2^{freq}[k]) \end{bmatrix}, \quad (11)$$

where:

$$p_{1,2}^{freq}[k] = \frac{1}{R_{avg}} \cdot \frac{1}{M} \sum_{r=1}^{R_{avg}} \sum_{m=0}^{M-1} s_{1,2,r}^2[m, k]. \quad (12)$$

2.1.5. Computation of the OR/AND Masks

There are two approaches to construct the Blanking Masks:

- the OR approach is computed by a tensor-logical OR operation between the vector results of the time and frequency RFI detector, denoted as $\vee$, whereas
- the AND approach is computed analogously using a tensor-logical AND operation, and it is denoted as $\wedge$.

The OR and AND blanking masks are defined for every Polarimetric Kurtosis metric as:

$$B_{k_p}^{OR}[m, k] = b_p^{time}[m] \vee b_p^{freq}[k], \quad (13a)$$

$$B_{k_p}^{AND}[m, k] = b_p^{time}[m] \wedge b_p^{freq}[k], \quad (13b)$$

with $p = 1 \dots 4$, and:

$$\begin{bmatrix} b_1^{time}[m] \\ b_2^{time}[m] \\ b_3^{time}[m] \\ b_4^{time}[m] \end{bmatrix} = \left\{ \left| \begin{bmatrix} k_1^{time}[m] \\ k_2^{time}[m] \\ k_3^{time}[m] \\ k_4^{time}[m] \end{bmatrix} - 2 \right| < \alpha_{th}^{time} \right\}, \quad (14a)$$

$$\begin{bmatrix} b_1^{freq}[k] \\ b_2^{freq}[k] \\ b_3^{freq}[k] \\ b_4^{freq}[k] \end{bmatrix} = \left\{ \left| \begin{bmatrix} k_1^{freq}[k] \\ k_2^{freq}[k] \\ k_3^{freq}[k] \\ k_4^{freq}[k] \end{bmatrix} - 2 \right| < \alpha_{th}^{freq} \right\}, \quad (14b)$$

In the proposed implementation, a simplification of $B_{k_{3,4}}^{OR/AND}[m, k]$ (eqn. (13) for the 3rd and 4th Stokes parameters is used, which consists of flagging an RFI in the polarimetric channels if it is either in the 3rd or in the 4th Stokes parameter, as:

$$B_{pol}^{OR}[m, k] = B_{k_3}^{OR}[m, k] \cap B_{k_4}^{OR}[m, k], \quad (15a)$$

$$B_{pol}^{AND}[m, k] = B_{k_3}^{AND}[m, k] \cap B_{k_4}^{AND}[m, k]. \quad (15b)$$

The final OR and AND blanking masks are computed by intersecting the statistical and polarimetric masks as:

$$B_{1,2}^{OR}[m, k] = B_{k_{1,2}}^{OR}[m, k] \cap B_{pol}^{OR}[m, k], \quad (16a)$$

$$B_{1,2}^{AND}[m, k] = B_{k_{1,2}}^{AND}[m, k] \cap B_{pol}^{AND}[m, k]. \quad (16b)$$

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2.1.6. RFI Mitigation

- Signal Blanking

Before applying the blanking mask, either the *AND* or the *OR* masks must be selected. While the *OR* approach maximizes the remaining radiometric signal at the same time as it mitigates the RFI power, the *AND* one may perform better when the RFI signal is faint in both the time and frequency domains, but it may also excise a significant part of the desired signal. An intermediate metric has to be defined to choose between the *AND* or the *OR* approaches in real time. To do so, the fraction of the bins to be mitigated by the *OR* mask is calculated as:

$$\beta_{1,2} = \frac{1}{M} \cdot \frac{1}{K} \sum_{m=0}^{M-1} \sum_{k=0}^{K-1} B_{1,2}^{AND}[m, k], \quad (17)$$

consequently, the mitigated STFT can be defined as:

$$Z_r^{mit}[m, k] = \begin{cases} (Z_r \circ B_z^{OR})[m, k] & \text{if } \beta_z \geq \beta_{th} \\ (Z_r \circ B_z^{AND})[m, k] & \text{otherwise} \end{cases}, \quad (18)$$

where the input Z_r ($Z_r = X_r$ or Y_r) is the *OR* blanking mask if β_z is larger than a threshold value β_{th} , or the *AND* blanking mask otherwise.

- PMS RFI Mitigation

The mitigation of the power measurements is performed by means of a pulse blanking approach in the time domain. However, since the sensibility of the PMS to detect RFI signals is much worse than for the STFT, instead of using just the instantaneous power value from the PMS to infer the presence or not of RFI, the signal blanking mask is calculated directly from the temporal moments of the polarimetric kurtosis ($b_{1,2}[m]$). In the proposed system, since the samples of the PMS are at ~28 kHz, they must first be resampled at the same rate as that the temporal bins of the STFT.

The RFI mitigation power factors (γ_{z_r} , with $Z = X$ or Y) are calculated for each receiver representing the ratio between the power of the bins after mitigation and before, as:

$$\gamma_{z_r} = \frac{\sum_{m=0}^{M-1} \sum_{k=0}^{K-1} |Z_r^{mit}[m, k]|^2}{\sum_{m=0}^{M-1} \sum_{k=0}^{K-1} |Z_r[m, k]|^2}, \quad (19)$$

and after the mitigation of the corrupted PMS, the sum of PMS samples that have not been discarded has to be normalized by the gamma factor, in order to estimate properly the power in each channel/polarization:

$$P_{z_r}^{mit} = \gamma_{z_r} \cdot \sum_{m=0}^{M-1} P_{z_r}[m] \cdot b_{z_r}^{time}[m]. \quad (20)$$

- RFI detection flag

The proposed RFI detection flag is computed as the logical OR between the 'all-bin' polarimetric kurtosis metrics, and the first and second Stokes parameters *AND* blanking matrices, and it can be expressed as

$$d_{RFI} = V \left\{ \left[\begin{array}{c} k_1^{all}[m] \\ k_2^{all}[m] \\ k_3^{all}[m] \\ k_4^{all}[m] \end{array} \right] - 2 \right\} > \alpha_{th}^{all} \bigvee V_{\forall m, k} \overline{B_1^{AND}[m, k]} \bigvee V_{\forall m, k} \overline{B_2^{AND}[m, k]}, \quad (21)$$

where V is a vector logical or operator applied over all the elements of a vector or matrix.

The first element of the logical OR in eqn. (21) represents that an RFI signal is detected within the data set, if any of the polarimetric kurtosis deviates more than $\pm \alpha_{th}^{all}$ from the theoretical value of 2. The value of α_{th}^{all} is selected to set the Constant False Alarm Rate or CFAR ($P_{FA} = \text{constant}$):

$$P_{FA} = 1 - \text{erf} \left(\frac{\alpha_{th}}{4/N} \right), \quad (22)$$

where N is the number of samples.

3. Results

An extensive battery of simulations covering a wide range of parameters, and long enough to be statistically representative, is needed in order to select the optimize the algorithm performance. The following parameters must be optimized:

- K is the number of points of FFT. The initial value of K was 4096, but it was proposed to run simulations with $K = 16384, 4096, 2048, 1024, 256$, and then select the best K for the default CFAR and β_{th} .
- α_{th} is the RFI detection threshold for statistical and polarimetry metrics: temporal, spectral and all-bin moments. $\alpha_{th}(P_{FA})$ is obtained mathematically for each value of the CFAR.
- The following CFAR values were simulated for the selected value of K : $10^{-8}, 10^{-6}, 10^{-4}, 10^{-2}, 0.1, 0.5$.
- β_{th} is the maximum blanking threshold from 100% to 50%.

Simulations with 1200 realizations containing standard RFI intensity distributions, as provided by Zenithal Blue Technologies (ZBT), and based on SMOS detected RFI have been used. Figure 3 shows the actual RFI probability and cumulative density functions for SMOS as measured in 2013 and 2020, as well as the simulated ones.

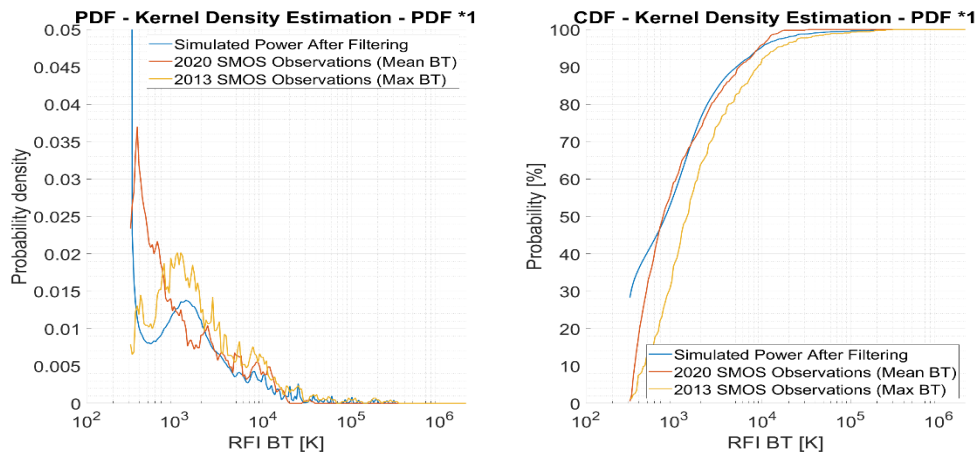


Figure 3. PDF (left) and CDF (right) of 2012 (yellow) and 2020 (orange) SMOS RFI observations. In blue simulated PDF and CDF.

3.1. Sensitivity Performance as a Function of the Number of Averages

An important consideration is the assessment of the sensitivity performance as a function of the number of averaged receivers, that is, assuming that each receiver has a system to compute the RFI mask, and input observables are averaged as described before. Figure 4 shows the reduction of the variance (ϵ) with respect to R_{avg} . As it can be appreciated in Figure 4a, for very low SNR values the variance reduction with respect to R_{avg} goes as $1/R_{avg}$, but as the SNR increases, the improvement (i.e., slope) decreases because of the signal correlation. For typical SMOS values, the typical SNR is $SNR_{typ} = 10 \cdot \log_{10}(|V|_{max}/T_R) \approx 10 \cdot \log_{10}(10 \text{ K}/210 \text{ K}) \approx -13 \text{ dB}$, being $|V|_{max}$ the maximum value of the visibility samples or cross-correlation in units of Kelvin, and therefore, the $1/R_{avg}$ approximation holds. Note that the use of 1-bit (Fig. 4b) instead of multibit (Fig. 4a) leads to a smaller variance reduction factor, i.e., it is even less sensitive to the SNR.

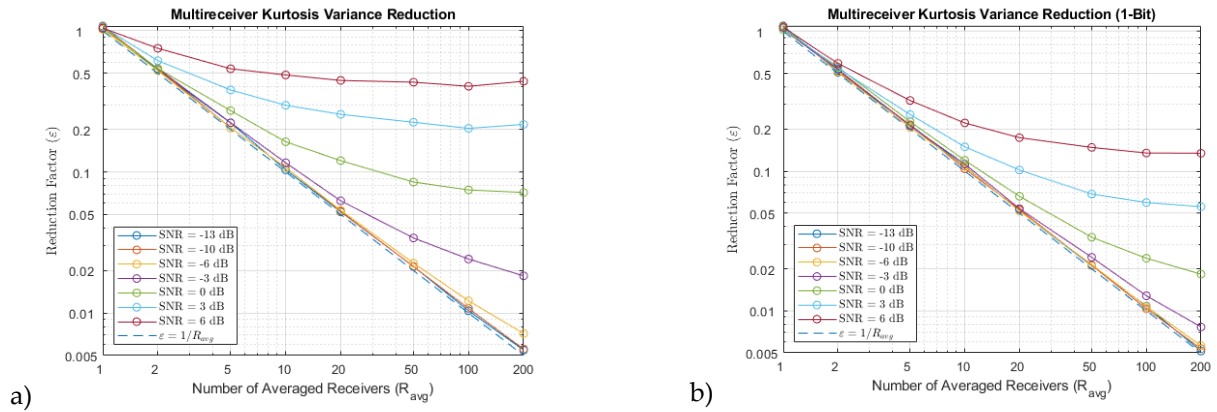


Figure 4. Multi-receiver Kurtosis variance reduction as a function of the number of receivers averaged (R_{avg}) and SNR for a) multi-bit, and b) 1-bit quantization. SNR is the power relation between correlated divided by uncorrelated noise power.

Figure 5 shows the Probability of Detection (P_D) of RFI vs. the Interference-to-Noise Ratio (INR). It shows a sudden increase above an INR value, which increases with increasing values of ϵ . As compared to the multi-bit case (Fig. 5a), in the case of 1-bit quantization (Fig. 5b), the plots are shifted ~ 2 dB towards the right due to larger noise ($10 \cdot \log_{10}(\sqrt{2.46}) \approx 1.95$ dB). Note that the 2.46 factor is the ratio of the integration time and the effective integration time for the case of 1-bit/2 levels correlators [19]. As shown in Fig. 6, these ~ 2 dB are nearly constant as a function of the number of receivers averaged.

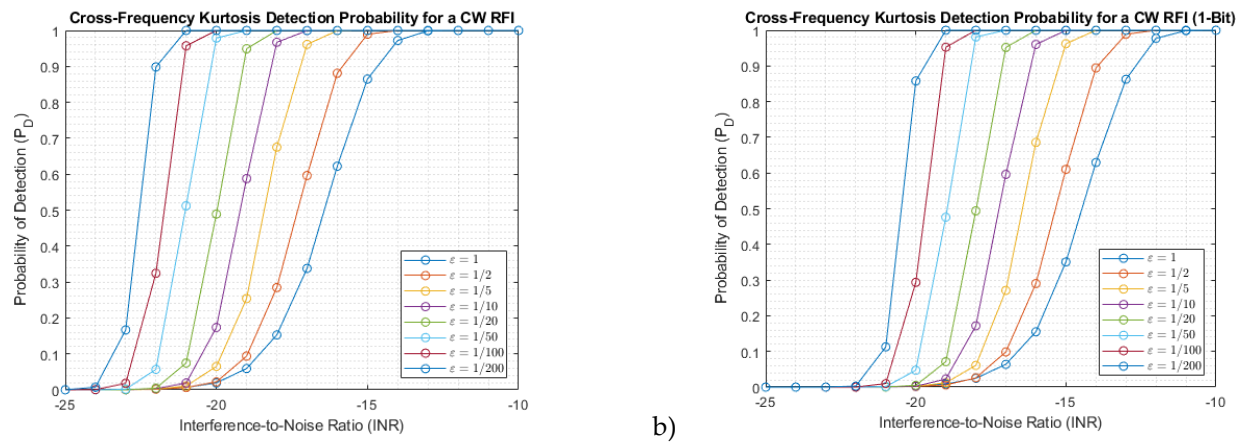


Figure 5. Probability of detection (PD) as a function of the INR, parameterized as a function of the variance reduction factor (ϵ), for (a) multi-bit, and (b) 1-bit quantization.

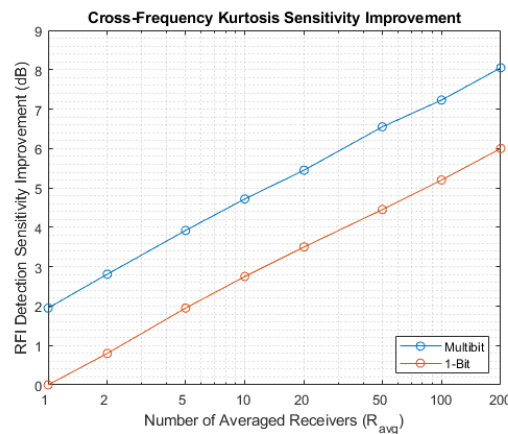


Figure 6. Sensitivity improvement of the RFI detection [dB] as a function of the number of receivers averaged (R_{avg}) for the multi-bit and 1-bit quantization approaches.

3.2. Algorithm Parameter Optimization

Numerical results are presented for the average (M), and the standard deviation (σ) of the mitigation for each value of K (length of the FFT), CFAR, and B_{th} . The percentage of mitigated RFI and degraded RFI (result is worse than no mitigation) are also provided, together with their mean values. In Tables 1-3 the range of values with similar performance, i.e., where the optimum is, is indicated in light blue color. In Table 4 the effect of the number of points of the FFT is clearly seen: the longer the FFT, the larger the PD, between 73-76%, for PFA < 1%, and K = 4096; between 70-72%, for PFA < 1%, and K = 2048; and ~59% for PFA < 1%, and K = 1024.

Table 1. Algorithm performance metrics for K = 4096 and variable CFAR and B_{th} .

K-FFT 4096	β_{th} 100%			β_{th} 90%			β_{th} 75%			β_{th} 50%		
	All #1200	Mitigating (<0)	Degrading (>0)	All #1200	Mitigating (<0)	Degrading (>0)	All #1200	Mitigating (<0)	Degrading (>0)	All #1200	Mitigating (<0)	Degrading (>0)
CFAR	M: -2,31 dB	% It. 59,3%	% It. 7,35%	M: -2,58 dB	% It. 56,2%	% It. 10,4%	M: -2,58 dB	% It. 56,2%	% It. 10,4%	M: -2,58 dB	% It. 56,2%	% It. 10,4%
10^{-8}	σ : 3,73 dB	M: -4,04 dB	M: 1,14 dB	σ : 5,05 dB	M: -5,48 dB	M: 4,80 dB	σ : 5,05 dB	M: -5,48 dB	M: 4,80 dB	σ : 5,05 dB	M: -5,48 dB	M: 4,80 dB
CFAR	M: -2,33 dB	% It. 60,8%	% It. 7,65%	M: -2,56 dB	% It. 57,5%	% It. 11,0%	M: -2,56 dB	% It. 57,5%	% It. 11,0%	M: -2,56 dB	% It. 57,5%	% It. 11,0%
10^{-6}	σ : 3,75 dB	M: -3,97 dB	M: 1,10 dB	σ : 5,11 dB	M: -5,41 dB	M: 4,98 dB	σ : 5,12 dB	M: -5,41 dB	M: 4,98 dB	σ : 5,12 dB	M: -5,41 dB	M: 4,98 dB
CFAR	M: -2,35 dB	% It. 62,2%	% It. 7,94%	M: -2,52 dB	% It. 58,2%	% It. 11,9%	M: -2,52 dB	% It. 58,2%	% It. 11,9%	M: -2,52 dB	% It. 58,2%	% It. 11,9%
10^{-4}	σ : 3,82 dB	M: -3,92 dB	M: 1,10 dB	σ : 5,24 dB	M: -5,39 dB	M: 5,24 dB	σ : 5,24 dB	M: -5,39 dB	M: 5,24 dB	σ : 5,24 dB	M: -5,39 dB	M: 5,24 dB
CFAR	M: 5,88 dB	% It. 69,0%	% It. 28,9%	M: 6,24 dB	% It. 63,5%	% It. 34,4%	M: 6,24 dB	% It. 63,5%	% It. 34,4%	M: 6,24 dB	% It. 63,5%	% It. 34,4%
10^{-2}	σ : 27,8 dB	M: -3,28 dB	M: 28,16 dB	σ : 29,3 dB	M: -4,98 dB	M: 27,3 dB	σ : 29,3 dB	M: -4,98 dB	M: 27,3 dB	σ : 29,3 dB	M: -4,98 dB	M: 27,3 dB
CFAR	M: 6,35 dB	% It. 73,6%	% It. 26,4%	M: 12,0 dB	% It. 41,3%	% It. 58,7%	M: 12,0 dB	% It. 41,3%	% It. 58,7%	M: 12,0 dB	% It. 41,3%	% It. 58,7%
10^{-1}	σ : 28,3 dB	M: -2,86 dB	M: 32,0 dB	σ : 33,0 dB	M: -5,04 dB	M: 23,9 dB	σ : 33,0 dB	M: -5,04 dB	M: 23,9 dB	σ : 33,0 dB	M: -5,04 dB	M: 23,9 dB

Table 2. Algorithm performance metrics for K = 2048 and variable CFAR and β_{th} .

K-FFT 2048	β_{th} 100%			β_{th} 90%			β_{th} 75%			β_{th} 50%		
	All	Mitigating	Degrading	All	Mitigating	Degrading	All	Mitigating	Degrading	All	Mitigating	Degrading
	#1200	(<0)	(>0)	#1200	(<0)	(>0)	#1200	(<0)	(>0)	#1200	(<0)	(>0)
CFAR 10^{-8}	M: -2,21 dB	% It. 57,3%	% It. 7,31%	M: -2,20 dB	% It. 56,2%	% It. 12,0%	M: -2,20 dB	% It. 56,2%	% It. 12,0%	M: -2,20 dB	% It. 56,2%	% It. 12,0%
	σ : 3,72 dB	M: -4,02 dB	M: 1,26 dB	σ : 5,20 dB	M: -5,46 dB	M: 5,57 dB	σ : 5,20 dB	M: -5,46 dB	M: 5,57 dB	σ : 5,20 dB	M: -5,46 dB	M: 5,57 dB
CFAR 10^{-6}	M: -2,24 dB	% It. 58,4%	% It. 7,72%	M: -2,19 dB	% It. 57,5%	% It. 12,6%	M: -2,19 dB	% It. 57,5%	% It. 12,6%	M: -2,19 dB	% It. 57,5%	% It. 12,6%
	σ : 3,77 dB	M: -4,01 dB	M: 1,26 dB	σ : 5,30 dB	M: -5,45 dB	M: 5,72 dB	σ : 5,30 dB	M: -5,45 dB	M: 5,72 dB	σ : 5,30 dB	M: -5,45 dB	M: 5,72 dB
CFAR 10^{-4}	M: -2,20 dB	% It. 60,3%	% It. 8,29%	M: -2,06 dB	% It. 58,2%	% It. 14,1%	M: -2,06 dB	% It. 58,2%	% It. 14,1%	M: -2,06 dB	% It. 58,2%	% It. 14,1%
	σ : 4,72 dB	M: -3,95 dB	M: 2,09 dB	σ : 6,08 dB	M: -5,39 dB	M: 6,24 dB	σ : 6,08 dB	M: -5,39 dB	M: 6,24 dB	σ : 6,08 dB	M: -5,39 dB	M: 6,24 dB
CFAR 10^{-2}	M: 5,79 dB	% It. 66,9%	% It. 30,5%	M: 6,52 dB	% It. 63,5%	% It. 36,5%	M: 6,52 dB	% It. 63,5%	% It. 36,5%	M: 6,52 dB	% It. 63,5%	% It. 36,5%
	σ : 26,6 dB	M: -2,83 dB	M: 25,2 dB	σ : 28,8 dB	M: -4,88 dB	M: 26,1 dB	σ : 28,8 dB	M: -4,88 dB	M: 26,1 dB	σ : 28,8 dB	M: -4,88 dB	M: 26,1 dB
CFAR 10^{-1}	M: 6,50 dB	% It. 72,9%	% It. 27,1%	M: 12,2 dB	% It. 41,3%	% It. 59,8%	M: 12,2 dB	% It. 41,3%	% It. 59,8%	M: 12,2 dB	% It. 41,3%	% It. 59,8%
	σ : 28,2 dB	M: -2,66 dB	M: 31,2 dB	σ : 32,9 dB	M: -5,02 dB	M: 23,8 dB	σ : 32,9 dB	M: -5,02 dB	M: 23,8 dB	σ : 32,9 dB	M: -5,02 dB	M: 23,8 dB

Table 3. Algorithm performance metrics for K = 1024 and variable CFAR and β_{th} .

K-FFT 1024	β_{th} 100%			β_{th} 90%			β_{th} 75%			β_{th} 50%		
	All	Mitigating	Degrading	All	Mitigating	Degrading	All	Mitigating	Degrading	All	Mitigating	Degrading
	#1200	(<0)	(>0)	#1200	(<0)	(>0)	#1200	(<0)	(>0)	#1200	(<0)	(>0)
CFAR 10^{-8}	M: -1,76 dB	% It. 48,8%	% It. 6,73%	M: -2,08 dB	% It. 46,8%	% It. 8,73%	M: -2,08 dB	% It. 46,8%	% It. 8,73%	M: -2,08 dB	% It. 46,8%	% It. 8,73%
	σ : 3,30 dB	M: -3,79 dB	M: 1,35 dB	σ : 4,67 dB	M: -5,36 dB	M: 4,92 dB	σ : 4,67 dB	M: -5,36 dB	M: 4,92 dB	σ : 4,67 dB	M: -5,36 dB	M: 4,92 dB
CFAR 10^{-6}	M: -1,73 dB	% It. 50,1%	% It. 7,26%	M: -2,06 dB	% It. 47,9%	% It. 9,54%	M: -2,06 dB	% It. 47,9%	% It. 9,54%	M: -2,06 dB	% It. 47,9%	% It. 9,54%
	σ : 3,30 dB	M: -3,64 dB	M: 1,34 dB	σ : 4,73 dB	M: -5,30 dB	M: 4,96 dB	σ : 4,73 dB	M: -5,30 dB	M: 4,96 dB	σ : 4,73 dB	M: -5,30 dB	M: 4,96 dB
CFAR 10^{-4}	M: -1,08 dB	% It. 51,2%	% It. 9,16%	M: -1,43 dB	% It. 49,1%	% It. 11,2%	M: -1,43 dB	% It. 49,1%	% It. 11,2%	M: -1,43 dB	% It. 49,1%	% It. 11,2%
	σ : 8,32 dB	M: -3,46 dB	M: 7,52 dB	σ : 9,05 dB	M: -5,21 dB	M: 10,1 dB	σ : 9,05 dB	M: -5,21 dB	M: 10,1 dB	σ : 9,05 dB	M: -5,21 dB	M: 10,1 dB
CFAR 10^{-2}	M: 8,19 dB	% It. 63,9%	% It. 35,7%	M: 8,57 dB	% It. 60,9%	% It. 38,7%	M: 8,58 dB	% It. 60,9%	% It. 38,7%	M: 8,58 dB	% It. 60,9%	% It. 38,7%
	σ : 28,5 dB	M: -1,86 dB	M: 26,2 dB	σ : 31,5 dB	M: -4,37 dB	M: 29,1 dB	σ : 31,5 dB	M: -4,37 dB	M: 29,1 dB	σ : 31,5 dB	M: -4,37 dB	M: 29,1 dB
CFAR 10^{-1}	M: 8,87 dB	% It. 69,7%	% It. 30,3%	M: 14,7 dB	% It. 37,5%	% It. 62,5%	M: 14,7 dB	% It. 37,5%	% It. 62,5%	M: 14,7 dB	% It. 37,5%	% It. 62,5%
	σ : 30,7 dB	M: -2,04 dB	M: 33,3 dB	σ : 35,8 dB	M: -4,84 dB	M: 26,4 dB	σ : 35,8 dB	M: -4,84 dB	M: 26,4 dB	σ : 35,8 dB	M: -4,84 dB	M: 26,4 dB

Table 4. Summary of algorithm performance in terms of PD and PFA for K = 4096, 2048 and 1024, and variable CFAR for $\beta_{th}=100\%$.

CFAR	K-FFT 4096		K-FFT 2048		K-FFT 1024	
	P_{FA}	P_D	P_{FA}	P_D	P_{FA}	P_D
10^{-8}	< 1%	73,1%	< 1%	69,8%	< 1%	59,4%
10^{-6}	< 1%	74,7%	< 1%	71,7%	6%	64,2%
10^{-4}	< 1%	76,2%	1%	74,5%	68%	81,8%
10^{-2}	87%	97,1%	91%	97,1%	100%	100%
10^{-1}	100%	100%	100%	100%	100%	100%

From the above results, the value of K = 1024 is selected, as it is a good trade-off between the computational complexity of the FFTs, and the algorithm's performance, with negligible P_{FA} , and reasonable probability of detection. The values of the CFAR and β_{th} parameters are now refined for K=1024. Results are presented in Table 5, confirming the optimum values of CFAR = 10^{-8} , and $\beta_{th} = 100\%$.

Table 5. Algorithm performance metrics for K = 1024, and variable CFAR and β_{th} .

K-FFT 1024	β_{th} 100%			β_{th} 99%			β_{th} 95%			β_{th} 90%		
	All	Mitigating	Degrading	All	Mitigating	Degrading	All	Mitigating	Degrading	All	Mitigating	Degrading
	#1200	(<0)	(>0)	#1200	(<0)	(>0)	#1200	(<0)	(>0)	#1200	(<0)	(>0)
CFAR 10^{-8}	M: -2.00 dB	% It. 52.0%	% It. 7.65%	M: -2.04 dB	% It. 48.6%	% It. 11.1%	M: -1.85 dB	% It. 47.7%	% It. 11.9%	M: -1.85 dB	% It. 47.7%	% It. 11.9%
	σ : 3.69 dB	M: -4.03 dB	M: 1.16 dB	σ : 5.16 dB	M: -5.48 dB	M: 5.62 dB	σ : 5.19 dB	M: -5.36 dB	M: 5.95 dB	σ : 5.18 dB	M: -5.36 dB	M: 5.95 dB
CFAR 10^{-6}	M: -2.00 dB	% It. 52.4%	% It. 7.81%	M: -2.05 dB	% It. 48.8%	% It. 11.4%	M: -1.85 dB	% It. 48.0%	% It. 12.2%	M: -1.85 dB	% It. 48.0%	% It. 12.2%
	σ : 3.68 dB	M: -4.00 dB	M: 1.15 dB	σ : 5.21 dB	M: -5.50 dB	M: 5.57 dB	σ : 5.21 dB	M: -5.35 dB	M: 5.90 dB	σ : 5.21 dB	M: -5.35 dB	M: 5.90 dB
CFAR 10^{-4}	M: -1.99 dB	% It. 52.4%	% It. 8.01%	M: -2.04 dB	% It. 48.8%	% It. 11.6%	M: -1.83 dB	% It. 48.0%	% It. 12.4%	M: -1.83 dB	% It. 48.0%	% It. 12.4%
	σ : 3.68 dB	M: -3.97 dB	M: 1.13 dB	σ : 5.23 dB	M: -5.50 dB	M: 5.61 dB	σ : 5.23 dB	M: -5.35 dB	M: 5.93 dB	σ : 5.22 dB	M: -5.35 dB	M: 5.93 dB
CFAR 10^{-2}	M: -1.98 dB	% It. 52.7%	% It. 8.15%	M: -2.03 dB	% It. 49.1%	% It. 11.8%	M: -1.83 dB	% It. 48.2%	% It. 12.6%	M: -1.82 dB	% It. 48.2%	% It. 12.6%
	σ : 3.67 dB	M: -3.94 dB	M: 1.12 dB	σ : 5.26 dB	M: -5.50 dB	M: 5.65 dB	σ : 5.25 dB	M: -5.35 dB	M: 5.97 dB	σ : 5.25 dB	M: -5.35 dB	M: 5.97 dB
CFAR 10^{-1}	M: -1.99 dB	% It. 53.3%	% It. 8.22%	M: -2.03 dB	% It. 49.3%	% It. 12.2%	M: -1.81 dB	% It. 48.5%	% It. 13.0%	M: -1.81 dB	% It. 48.5%	% It. 13.0%
	σ : 3.69 dB	M: -3.92 dB	M: 1.16 dB	σ : 5.29 dB	M: -5.50 dB	M: 5.60 dB	σ : 5.29 dB	M: -5.34 dB	M: 5.95 dB	σ : 5.28 dB	M: -5.34 dB	M: 5.95 dB

Table 6 summarizes the algorithm performance in terms of P_D and P_{FA} . Note that the P_D value is slightly higher than in Table 4 due to the finite number of realizations conducted (1200).

Table 6. Summary of algorithm performance in terms of PD and PFA for K = 1024, and variable CFAR for β_{th} = 100%.

CFAR	K-FFT 1024	
	P_{FA}	P_D
10^{-8}	< 1%	63.5%
$3 \cdot 10^{-8}$	~2%	64.1%
10^{-7}	~2%	64.6%
$3 \cdot 10^{-7}$	~2%	66.2%
10^{-6}	6%	67.7%

As a summary, the optimum parameters are:

- K = 1024, no significant improvement is found for larger K's except a better P_D (from 63 to 73%), at the expense of more hardware resources to compute the FFTs.
- CFAR = 10^{-8} , with no significant variation up to 10^{-6} , with a moderate P_D , and a negligible PFA (not detectable with the number of realizations performed). This offers less radiometric degradation, and no big impact on mitigation.
- β_{th} = 100%. No significant impact down to 95%, but 100% offers the best mitigation vs. degradation trade-off.

RFI mitigation results are summarized in Figure 7, both for the cross-correlations, and for the PMS output.

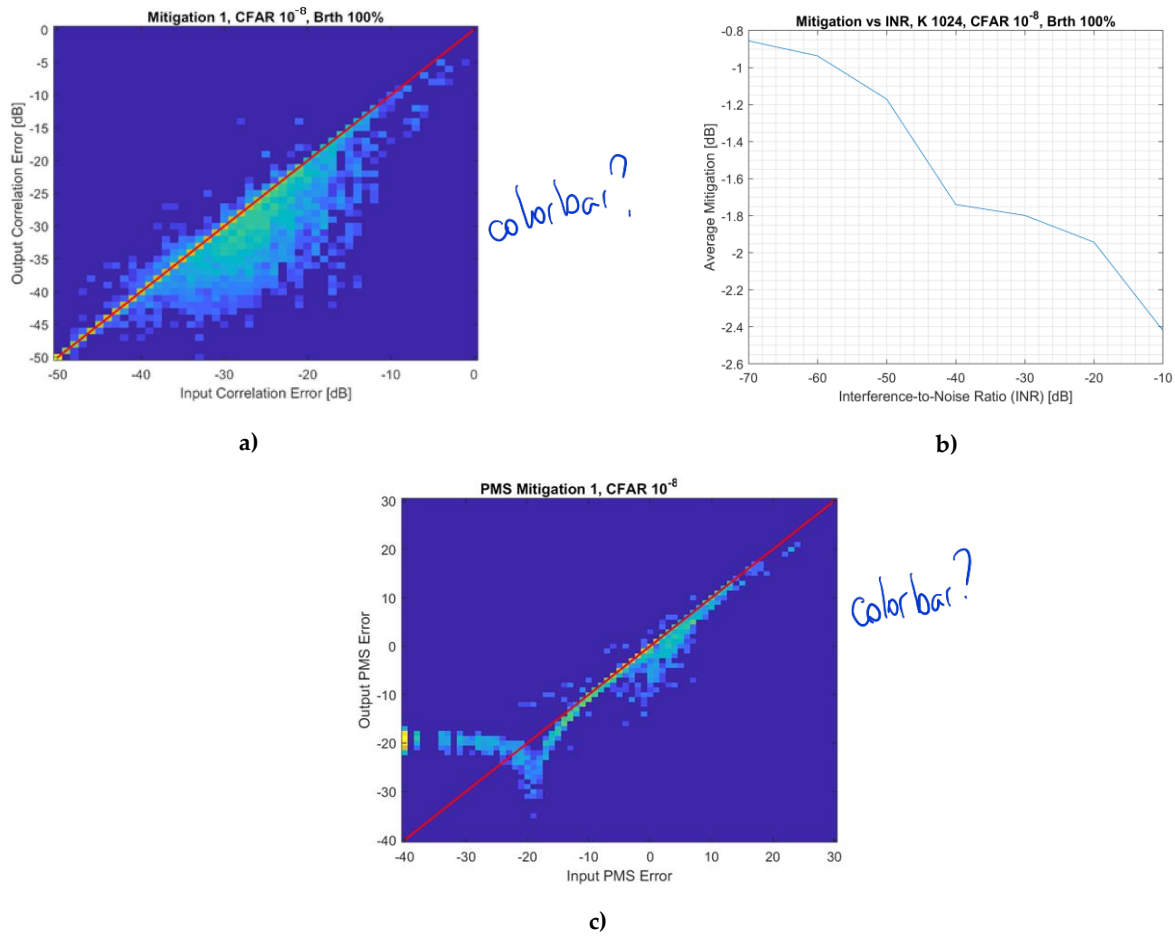


Figure 7. a) Detection regimes after applying the algorithm, b) Average mitigation [dB] wrt. input INR [dB], c) Input-output PMS error for CFAR = 10⁻⁸ and Bth = 100%.

4. Discussion

In the previous Sections, the calculation of the Stokes parameters per frequency bin in the Short Time Fourier Transform (STFT), and the Polarimetric Kurtosis the Polarimetric Kurtosis have been introduced as key steps towards an efficient RFI detection and mitigation algorithm in Synthetic Aperture Interferometric Radiometers, using 1-bit quantization, as in SMOS and planned follow-on missions.

After RFI mitigation, the signals are in the frequency domain, so their complex-correlation can be computed either transforming them back to the time domain, or in the frequency domain, thanks to the Parseval's Theorem:

$$\sum_{n=0}^{N-1} x_r[n] \cdot y_r^*[n] = \sum_{m=0}^{M-1} \sum_{k=0}^{K-1} X_r[m, k] \cdot Y_r^*[m, k]. \quad (23)$$

On the other hand, implementing the correlations with multipliers with a large number of bits is very resource-consuming. Two alternatives are discussed here:

- Quantization of the signals in the frequency-domain and perform the products with a reduced number of bits (1 to 5), so that multipliers can be more easily implemented using look-up tables (LUT).
- Transform the signals back to the time domain, quantize the signals in the time-domain, and perform the products with a reduced number of bits (1 to 5).

Quantization introduces a non-linear effect between the ideal “analog” correlation and the one computed using quantized signals. These effects were introduced in [19] and analyzed in more depth in [22, 23]. However, for small correlation values, the relationship is almost linear, and just a slope correction factor is required (1.0092 for 5 bits, 1.0321 for

4 bits, 1.1128 for 3 bits, 1.1558 for 2 bits, and 3.3670 for 1-bit), although it also amplifies the noise in the measurements (see Appendix 1).

Simulation results for the frequency-domain and time-domain correlations with different number of bits are shown in Fig. 8a and 8b. The vertical grey lines represent the 16-bit quantization noise floor: $10 \cdot \log_{10}(2^{-16}) + 40 = -8.16$ dBcu (1 cu = 10^{-4} = 1 correlator unit) as in SMOS. The horizontal lines represent the quantization noise floor for the different quantization levels. As it can be appreciated, for a virtually infinite number of levels (top left scatter plot) there is no saturation effect. As the number of quantization bits (levels) decreases (5 to 1 bits: 31 to 2 levels) a saturation effect appears at increasing levels: for 31 levels, the saturation occurs very close to the SMOS quantization noise floor, and increases at $\sim +3$ dB for every bit that is decreased. Note that the performance is significantly worse when the correlation is performed in the time domain, due to the fact that the truncation to compute the FFTs already spreads the spectra, and the subsequent truncation degrades it even further.

The above results are summarized in Table 7 showing that the performance of computing the cross-correlations in the frequency domain is much more efficient in terms of mitigation for 31, 15 and even 7 quantization levels, with actually very similar performances, and only approached by the cross-correlation in the time domain with 31 levels, although it mitigates in a smaller fraction of samples and degrades it in a larger fraction.

Table 7. Comparison results for the different correlator architectures under consideration. In green: optimum values.

Correlation	All [1200 it.]		Mitigating (<0)		Degrading (>0)	
FRef	Mean -3,00 dB	Std 4,22 dB	% It. 57,5%	Mean -4,36 dB	% It. 4,6%	Mean 1,82 dB
FQ31	Mean -3,28 dB	Std 4,25 dB	% It. 65,9%	Mean -4,04 dB	% It. 10,8%	Mean 1,00 dB
FQ15	Mean -3,37 dB	Std 4,28 dB	% It. 65,6%	Mean -4,21 dB	% It. 11,7%	Mean 1,14 dB
FQ7	Mean -3,35 dB	Std 4,35 dB	% It. 64,1%	Mean -4,39 dB	% It. 13,5%	Mean 1,49 dB
FQ3	Mean -2,73 dB	Std 4,45 dB	% It. 59,9%	Mean -4,24 dB	% It. 17,7%	Mean 2,33 dB
FQ2	Mean 0,06 dB	Std 5,27 dB	% It. 40,1%	Mean -3,92 dB	% It. 37,6%	Mean 4,32 dB
TRefFFT	Mean -3,10 dB	Std 4,31 dB	% It. 64,6%	Mean -3,85 dB	% It. 12,3%	Mean 0,67 dB
TQ31	Mean -3,33 dB	Std 4,89 dB	% It. 58,9%	Mean -4,88 dB	% It. 18,9%	Mean 1,50 dB
TQ15	Mean -1,88 dB	Std 5,00 dB	% It. 49,9%	Mean -4,34 dB	% It. 27,9%	Mean 2,53 dB
TQ7	Mean 0,99 dB	Std 5,74 dB	% It. 30,1%	Mean -4,34 dB	% It. 47,8%	Mean 4,35 dB
TQ3	Mean 2,03 dB	Std 5,82 dB	% It. 24,8%	Mean -4,13 dB	% It. 53,0%	Mean 4,91 dB
TQ2	Mean 12,04 dB	Std 7,14 dB	% It. 2,9%	Mean -3,28 dB	% It. 74,9%	Mean 12,64 dB

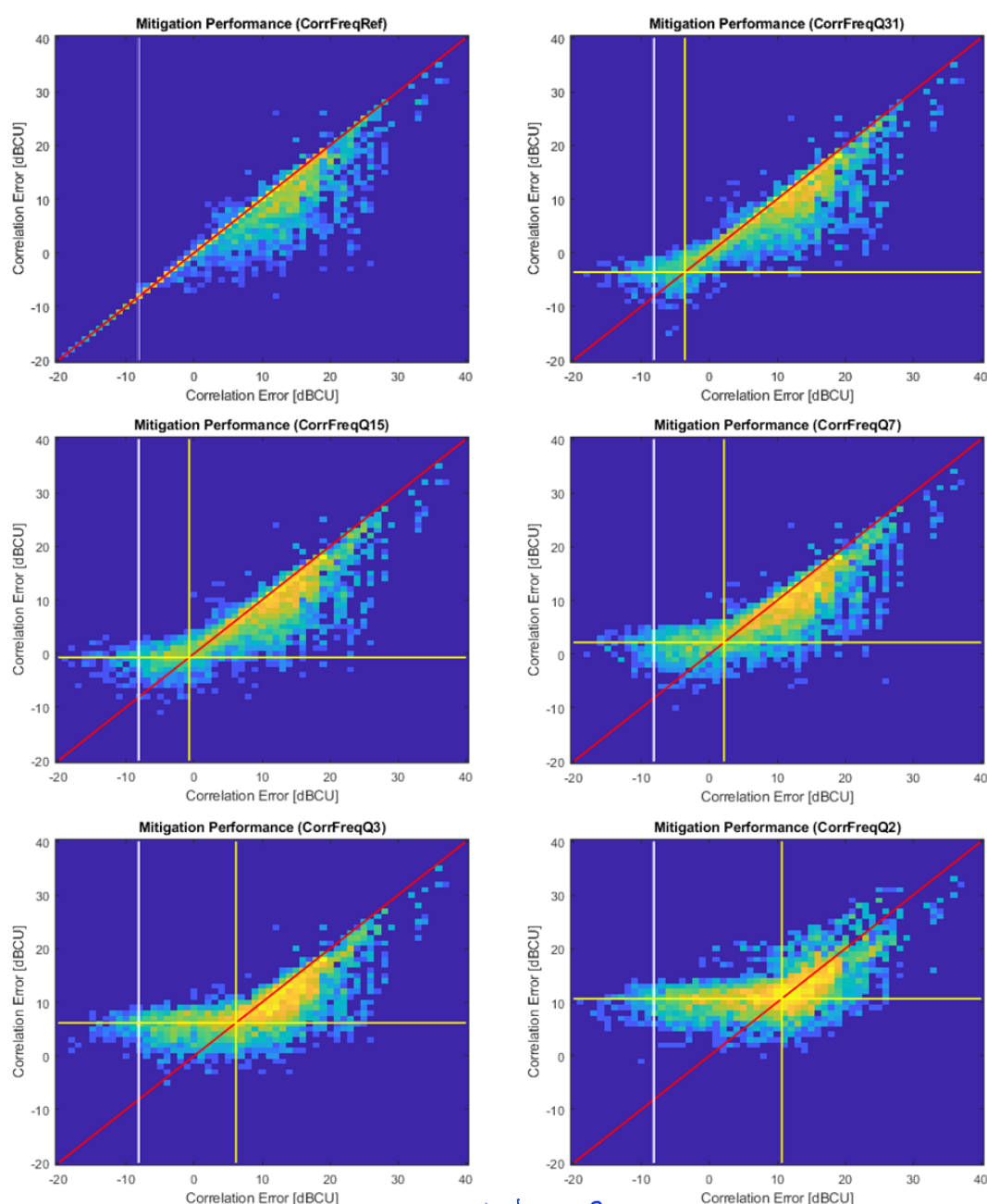
5. Conclusions

This study has presented a new RFI detection and mitigation algorithm for Synthetic Aperture Microwave Radiometers with coarse quantization schemes, such as the one planned for the SMOS follow-on mission. After signal windowing and channel equalization, statistical and polarimetric tests are applied in the time and/or frequency domains to detect the presence of RFI. As new features of this algorithm, it computes the Stokes parameters per frequency bin in the Short Time Fourier Transform (STFT), and also the so-called Polarimetric Kurtosis, for the 3rd and 4th Stokes parameters. Finally, when RFI is detected in one of these domains or both, blanking masks are calculated and applied to remove the RFI.

For a CFAR of 10^{-8} , it is found that the optimum parameters are: length of the FFTs equal to 1024 (without significant improvement found for larger values, except for a slightly better probability of detection: from 63 to 73%), β_{th} equal to 100% (i.e. only if the

AND approach does not mitigate at all, the OR approach is used), and application of Parseval's Theorem to compute the cross-correlations in the frequency domain using 31, 15 or even 7 quantization levels, with very similar performance among the three of them.

Finally, it is also worth mentioning that: 1) the algorithms presented can also be applied to (Polarimetric) Real Aperture Radiometers, despite $R_{avg} = 1$, and 2) algorithm's performance can be significantly improved if softer quantization schemes are used (i.e., more than 1-bit).



colorbars?

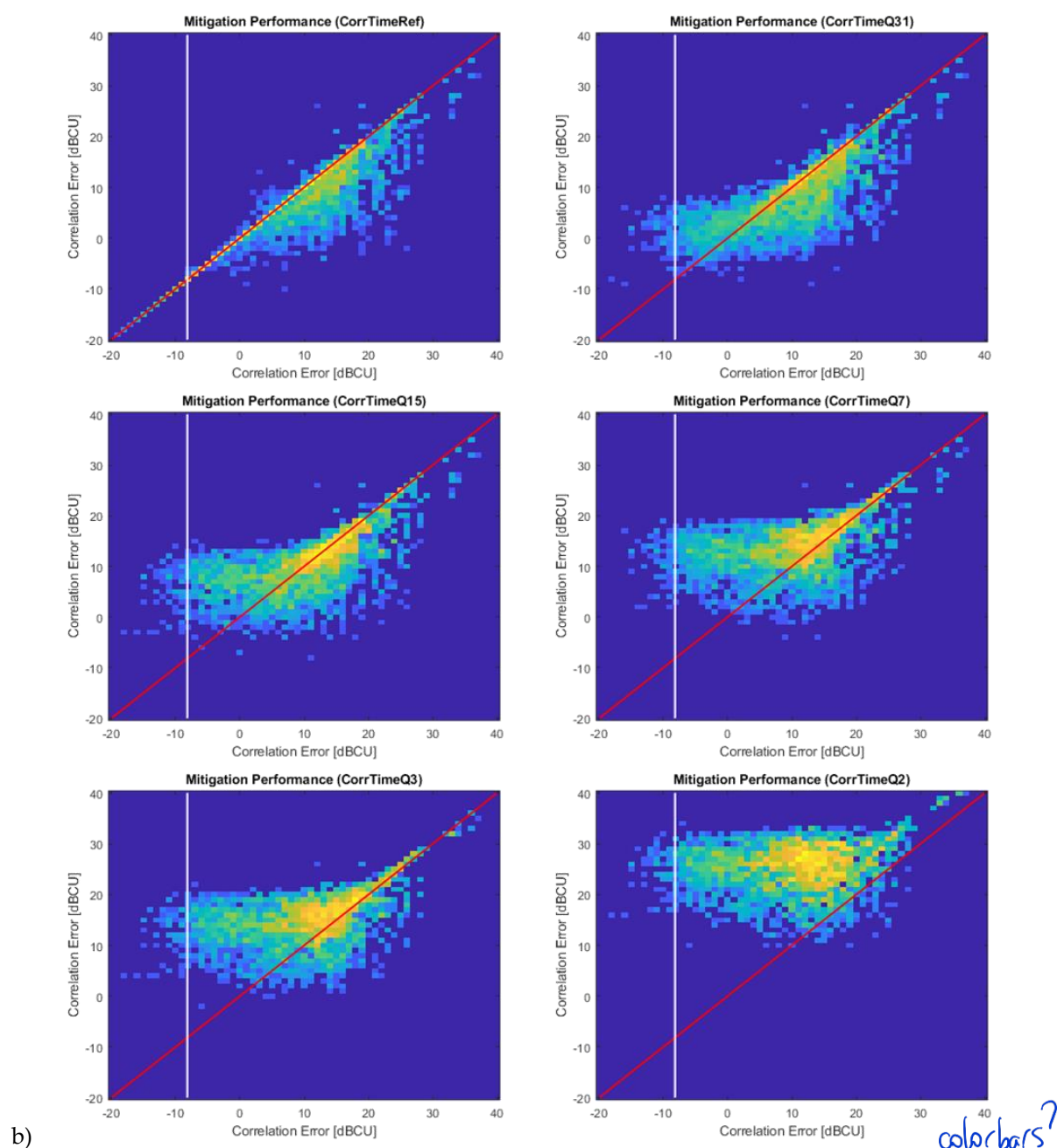


Figure 8. Mitigation performance in the a) frequency-, and b) time-domains as a function of the quantization levels: 2, 3, 7, 15, and 31 and multi-bit reference case (top left).

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Appendix 1: Quantization Effects and their Compensation

If after the STFT the real and imaginary parts are truncated at a maximum value of $\pm V_{Trunc} = \pm \delta \cdot \sigma_{x,y}$, being δ the scaling factor and $\sigma_{x,y}$ the standard deviation, the resulting spectra gets discretized. In principle, δ must be selected so that clipping effects are negligible. Figure A.1 shows the evolution of the RMSE in correlation units [CU] ($\times 10^{-4}$), computed as the root mean squared error between the cross-correlation and the reference cross-correlation in the time domain, for different the number of bits/levels used in the quantization:

$$RMSE = \sqrt{\sum |CorrX - CorrTimeRef|^2}. \quad (A.1)$$

For 1 bit/2levels (Q2), there is no sensitivity as the amplitude information is lost. For 2 bits/3 levels a narrow optimum exists around $\delta \approx 2$, and this valley flattens for increasing number of levels (i.e. bits). In these circumstances, the impact of δ is not as relevant as in an ADC the value of V_{Trunc} may be adjusted as a function of the estimated $\sigma_{x,y}$ to work in an optimal δ value.

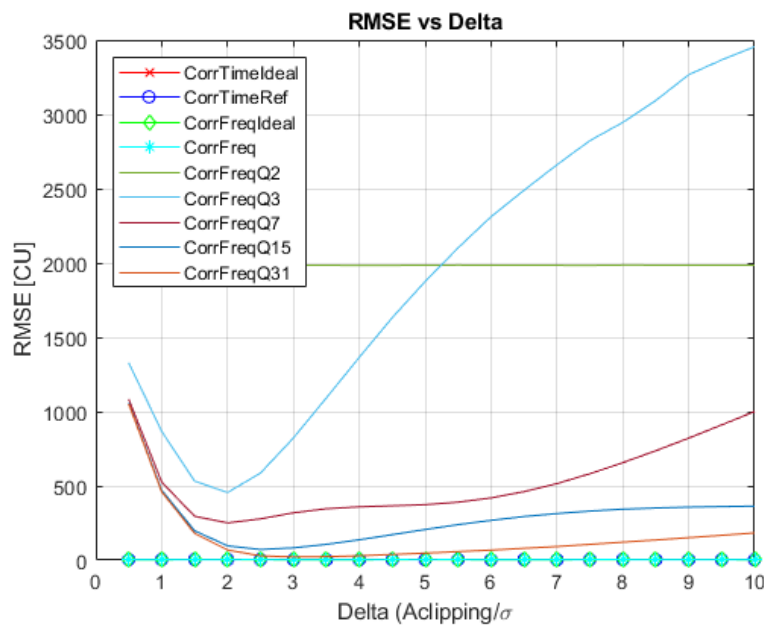


Figure A.1. Evolution of the RMSE in [CU] as a function of $\delta = V_{Trunc} / \sigma_{x,y}$ for different quantization levels.

Figure A.2 (left) shows the correlator transfer function for the ideal δ as a function of the ideal correlation value and different quantization schemes. Note that CorrFreqQ2 becomes the asin (inverse sine function) as in SMOS, if no filtering is performed at all. Figure A.2 (right) shows a zoom of Figure A.2a for values < 1000 CU showing that the relationship is nearly a straight line.

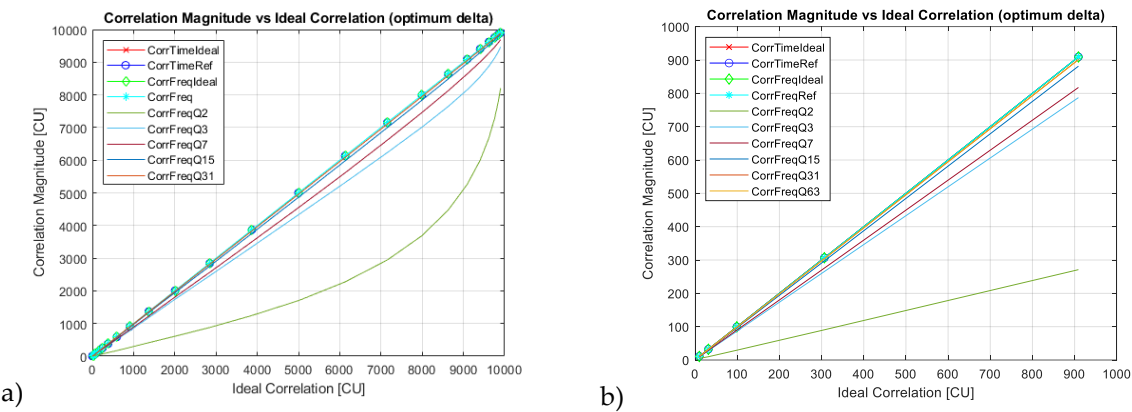


Figure A.2. Evolution of the RMSE in [CU] as a function of the $\delta = V_{Trunc} / \sigma_{x,y}$, for different quantization levels.

For values smaller than 1000 CU's, the slope correction factor is given in the following table.

Table A.1. Slope correction factor due to quantization scheme applied when cross-correlations are computed in the frequency domain. Note: the larger the slope correction, the larger the noise amplification.

	FQ31	FQ15	FQ7	FQ3	FQ2
Correct. Fact. (m ⁻¹)	1.0092	1.0321	1.1128	1.1558	3.3670