Manuscript Title:

The Effects of Internal Erosion on the Physical and Mechanical Properties of Tailings Under Heavy Rainfall Infiltration

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Abstract:

The stability of tailings dam will be affected by the internal erosion under unsteady seepage caused by heavy rainfall infiltration which changes the physical and mechanical properties of tailings. In this paper, the hydraulic sedimentary model was established to investigate the effects of dry beach slope on the sedimentary characteristics of tailings in upstream tailings dam, and the results indicated that the dry beach with a larger slope has a more obvious stratification of tailings. And the sand column model was built to investigate the effects of internal erosion on the physical and mechanical properties of sedimentary tailings under unsteady seepage, and the results indicated that the migration of fine-grained tailings was caused by internal erosion increases the permeability and reduces the shear strength of the tailings. After internal erosion of tailings under heavy rainfall in 50-years return period for 24h, the average particle size of downstream tailings(sample DT), midstream tailings(sample MT) and upstream tailings(sample UT) increased by 6.4%, 12.0% and 2.4% respectively, the hydraulic conductivity of sample DT, sample MT and sample UT increased by 27.2%,17.9%, and 15.3% respectively, and the shear strength of sample DT, sample MT and sample UT decreased by 20.9 %, 15.1% and 12.4% respectively.

Key words: Upstream tailings dam; Sedimentary characteristics; Unsteady seepage; Internal erosion; Particle size distribution; Hydraulic conductivity

1.Introduction

As the third-largest mining country, China produces about 300 million tons of tailings every year. And most of the tailings were stored in more than 2,000 tailings reservoirs. However, more than 20% of these hydraulic earth structures are at risk of dam failure, which has become one of the most dangerous sources for mining enterprises[1-2]. Serious tailings dam-failure accidents have happened all over the world. For example, tailings dam-failure accidents of Xinta Mining Company(Shanxi Province, China) in September 2008 claimed the deaths of 270 people and the direct economic loss of 96.19 million RMB Yuan[3]. On the 25th January 2019, the collapse of Córrego do Feijão tailing dam at Brumadinho city (Minas Gerais, Brazil), causing at least 12 million cubic meters of tailing were spread into Paraopeba River and the surrounding area, leaving over 250 people dead[4].

The United States Committee on Large Dams (USCOLD) evaluated the causes of dam-failure accidents, indicated that heavy rainfall was the critical factor that contributes to 30% of the dam-failure accidents[5-7]. When heavy rainfall infiltrates into the tailings, the saturation line of the tailings dam will rise rapidly, as shown in Fig.1. The rise of saturation line increases the hydrostatic pressure and the hydrodynamic pressure of tailings dam, which promotes seepage erosion and affects tailings' physical and mechanical properties. As a widely used dam construction method in China, the upstream tailings dam is more susceptible to internal erosion under heavy rainfall infiltration due to the fine-grained tailings located in the upstream of the seepage direction. The fine-grained tailings are easily carried away from the pore-channel of the coarse-grained tailings by seepage forces. Therefore, it is necessary to investigate the erosion mechanism and the effects of internal erosion on tailings' physical and mechanical properties under heavy rainfall infiltration.

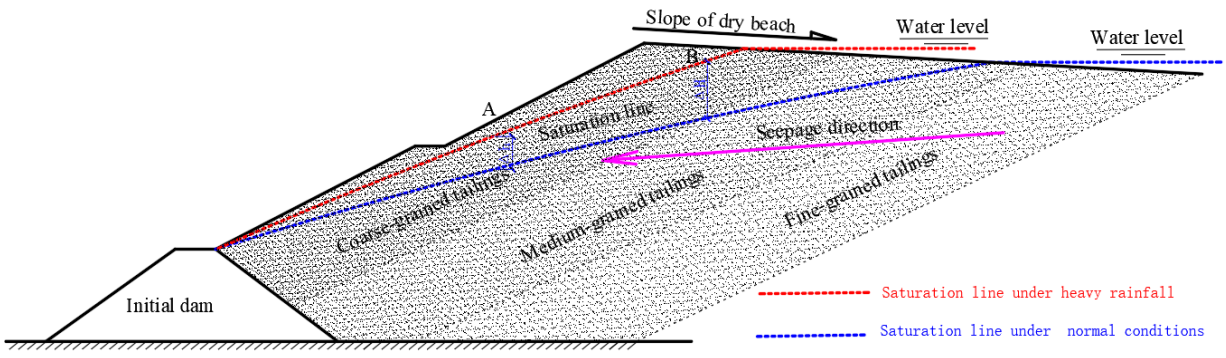


Fig. 1 Sedimentary and seepage characteristics of upstream tailings dam

For the past few years, numerous investigations have been conducted concerned with the effect of internal erosion on the soils. Chen et al. [8]investigated the migration trend of the fine particles in cohesionless soils and the change law of content of the remaining fine particles during the process of internal erosion. Zhang [9]established the numerical slope model to analyze the effects of internal erosion on the stability of the slope. Yao et al. [10]investigated the internal erosion mechanism of unstable embankment and analyzed the effect of the increasing water level and hydraulic conductivity on the stability of the embankment. Zhang et al. [11]proposed the prediction formula of the gravel soil's critical vertical upward hydraulic gradient based on the force balance theory of a particle group under internal erosion. Wilson et al. [12] investigated the impact of soil properties on internal erosion and built the streambank stability model to demonstrate the increase of bank's instability due to undercutting by internal erosion. Chu-Agor et al. [13]develop an empirical sediment transport function to predict internal erosion and undercutting of cohesive bank with time-based on three-dimensional soil block experiments. Ke et al. [14]performed a series of one-dimensional upward seepage tests at a constant water head to cause internal erosion in a soil sample and pointed out that internal erosion causes a significant increase in void ratio and hydraulic conductivity, resulting in a reduction of soil strength. Midgley et al. [15] performed the seepage research on a streambank of Dry Creek, and pointed out internal erosion plays an important role in the streambank failure, especially when acting in concert with fluvial erosion processes. Jiang et al. [16]used MICP technology to control the internal erosion of sand-clay mixtures by test apparatus in the laboratory and pointed out that MICP treatment facilitates the reduction of erosion and volumetric contraction of sand-clay mixtures. Liu et al. [17] designed a stress-controlled seepage test apparatus to study the failure mechanism and evolution characteristics of water-sand inrush caused by the instability of filling medium in karst cavity.

In profits from in predecessor's research foundation, the hydraulic sedimentary model of upstream tailings dam was established to analyze the sedimentary characteristics of tailings on the dry beach, and the unsteady seepage test was performed to investigate the effect of internal erosion on the physical and mechanical properties of tailings under heavy rainfall infiltration. The research results play an essential role in analyzing and predicting the impact of internal erosion on the stability of tailings dam.

2.Sedimentary characteristics of tailings at different dry beach slopes

The gradation, spatial distribution and porosity of tailings have an important influence on the internal erosion of tailings dam. The tailings in the upstream tailings dam show distinctive sedimentary characteristics along the dry beach slope during the discharge of tailings slurry, as shown in Fig.1. Therefore, it is necessary to analyze the sedimentary characteristics of the upstream tailings dam before investigating the effect of internal erosion on tailings dam under heavy rainfall.

2.1Experimental materials and model

2.1.1 Raw tailings

The raw tailings chosen in this experiment came from the discharge outlet of a tailings dam in southern China. The height of the tailings dam is 42.1m with a slope ratio of 1:4, and the length of the dry beach is 50m with a slope of 1% - 2%. The physical properties of the raw tailings were determined according to ASTM recommended test methods (ASTM D2216-19/ D854-14/ D7263-21) [18-20], as shown in Table 1.

Table 1. Physical properties of the raw tailings sample

Raw material	Natural density $\rho(g/cm^3)$	Moisture content ω (%)	Pore ratio e	Relative density G_s	Dry density $\rho_d(g/cm^3)$
Tailings sample	1.42	14.0	1.11	2.68	1.27

The particle characteristics of the raw tailings sample were analyzed by Screening Test, and the particle size smaller than 0.075 mm was determined by Winner2000 Laser Particle Size Analyzer[21]. The particle size distribution curve was plotted according to test results, as shown in Fig.2.

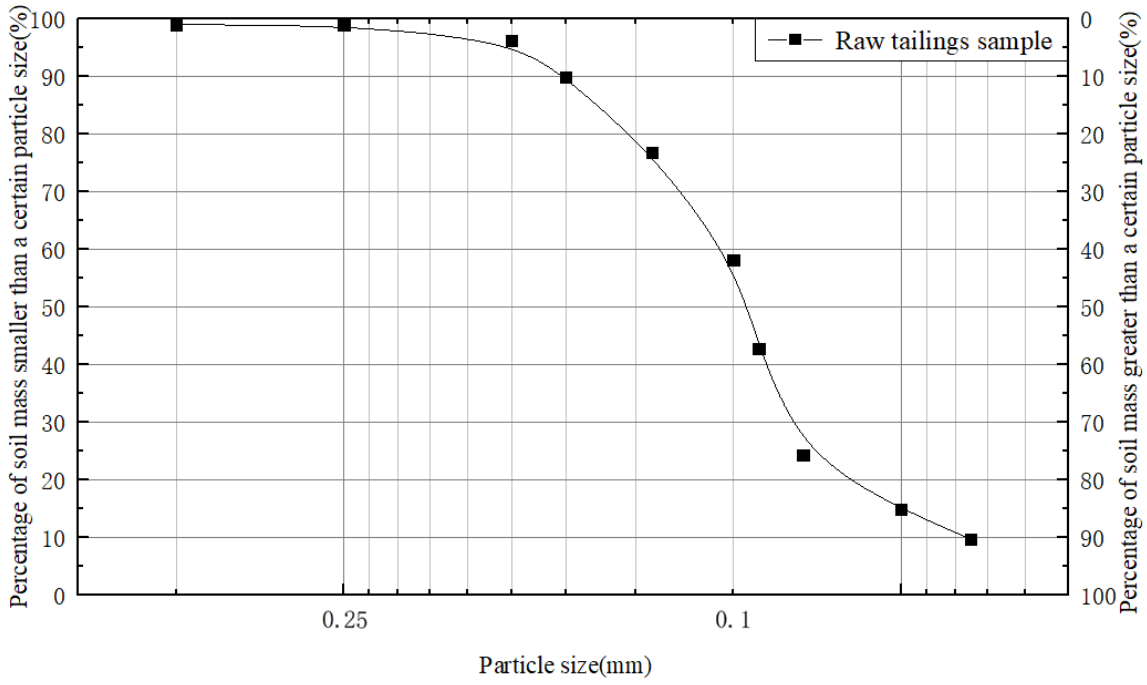


Fig. 2 Particle size distribution curve of raw tailings sample

The characteristic values of the raw tailings sample were calculated according to Fig.2, as shown in Table 2.

Table 2 The particle characteristics of raw tailings sample

Characteristic values	Effective particle size d_{10}(mm)	Median particle size d_{30} (mm)	Average particle size d_{50}(mm)	Restricted particle size d_{60}(mm)	Non-uniformity coefficient C_u	Curvature coefficient C_c
Raw tailings sample	0.031	0.092	0.097	0.102	3.33	2.66

2.1.2 Experimental model

A physical model for hydraulic sedimentation test of tailings was established to simulate the tailings discharge from the upstream tailings dam and to analyze the sedimentary characteristics of tailings on the dry beach. The main body of the model is a length of 500cm plastic groove with a Trapezoidal cross-section(30cm wide of the topline, 20cm wide of the baseline, and 10cm high) to simulate the dry beach of tailings dam. A height-adjustable cushion set at the upstream of the physical model was used to adjust the slope of the groove(1%-2%), which is consistent with the dry beach slope of the tailings dam. A plastics discharge pipe with an inner diameter of 0.3cm is installed at the bottom of the mixing tank to discharge the tailing slurry, as shown in Fig.3.

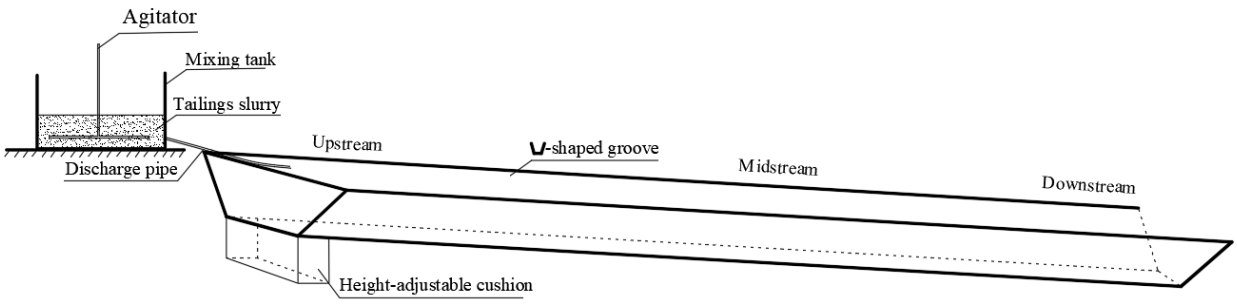


Fig.3 Schematic diagram of the physical model for the tailings hydraulic sedimentary test

According to the Froude criterion[22], when fluid flow is dominated by inertial force and gravitational force, the physical model and prototype of fluid should have the same Froude number to meet the dynamic similarity conditions. The Froude number is the ratio of inertial force to gravitational force during the process of fluid flow, as shown in Formula (1)

$$F_r = \frac{v}{\sqrt{gL}} \tag{1}$$

Where, F_r is the Froude number; g is gravity; v is water velocity; L is the flow length of fluid.

The flow of the tailings slurry on the dry beach is dominated by inertial force and gravitational force, so the physical model should have the same Froude number as the prototype, that is $F_{rm} = F_{rp}$.

$$\frac{v_m}{\sqrt{gL_m}} = \frac{v_p}{\sqrt{gL_p}} \tag{2}$$

$$\frac{L_p}{L_m} = \frac{v_p^{\,2}}{v_m^{\,2}} \tag{3}$$

Where, F_{rm}, L_m, v_m is the Froude number, length, water velocity of physical model; F_{rp}, L_p, v_p is the Froude number, dry beach length, water velocity of prototype

The similarity ratio of the hydraulic parameters between the physical model and the prototype was derived according to the Froude criterion, as shown in Table 3.

Table 3 The similarity ratio of the hydraulic parameters between the physical model and prototype

Parameters	Similar ratio
length	1:100
Fluid flow area	1:400
Flow rate	$1:100^{1/2}$
Volume flow	$1:200^{5/2}$

The actual flow rate of tailings slurry at the discharge outlet of the tailings dam is measured by a flow meter, which is1.72 m/s, as shown in Fig.4.



Fig.4. Flow rate of tailings at the discharge outlet

The hydraulic parameters for the physical model were calculated according to the actual flow rate. The mass ratio of water and tailings in the physical model is consistent with that of actual tailing slurry, as shown in Table 4

Table 4 The hydraulic parameters of the physical model

Similar parameters	Water velocity (cm/s)	Volume flow (m^3/s)	Mass ratio of water and tailings
Test values	17.2	1.21e-6	3:1

2.2Experimental procedures

(1)Adjust the height of the cushion to maintain the slope of the Trapezoidal groove at 1%.

(2)Put the tailings and water in the mixing tank at a mass ratio of 1:3. Stir the tailings slurry 10 minutes to uniform, and drain it into the Trapezoidal groove through the discharge pipe at the volume flow of 1.21e-6 m^3/s until the stacking height of upstream tailings exceeds 10cm.

(3)The tailings samples are taken from the downstream, midstream and upstream of the Trapezoidal groove when the water is completely drained out, numbered as sample DT, sample MT and sample UT.

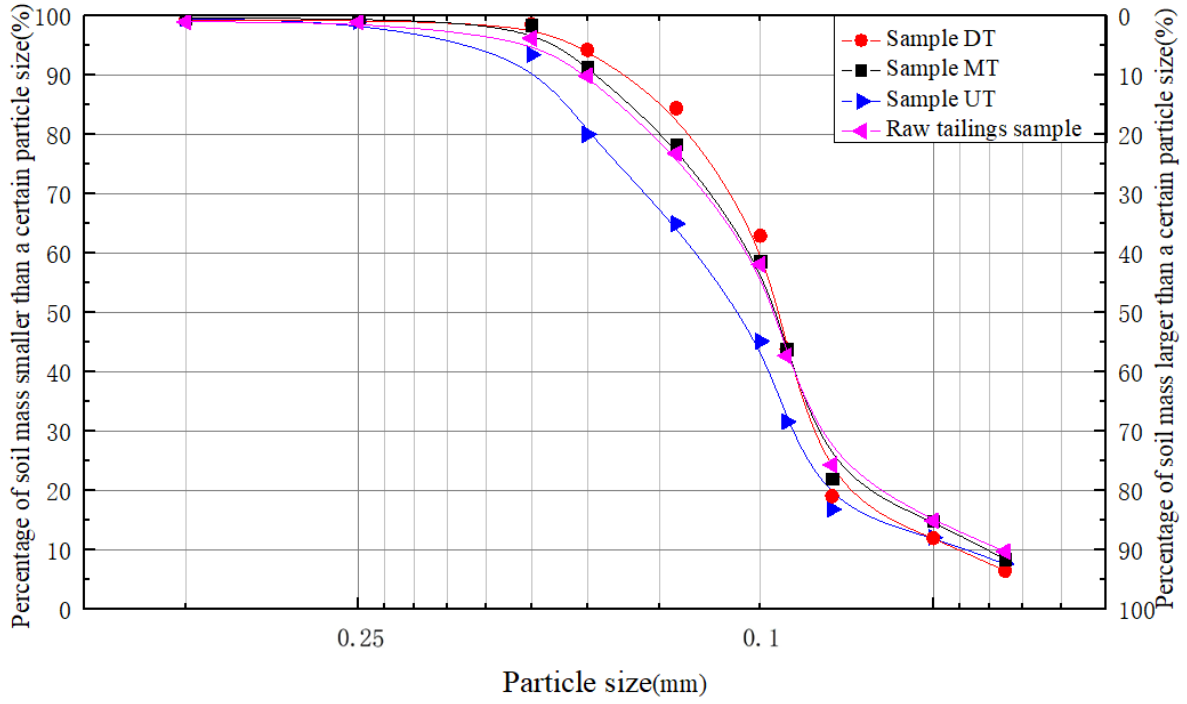
(4)Dry the tailings samples with a thermostatic drying chamber (105~110 ℃) for no less than 10h. The particle size distribution of each tailings sample is determined by Screening Test and Laser Particle Size Analysis.

(5)Change the slope of the Trapezoidal groove to 1.5% and 2.0% respectively by adjusting the height of the cushion, and repeat the procedures of step (2) to step (4).

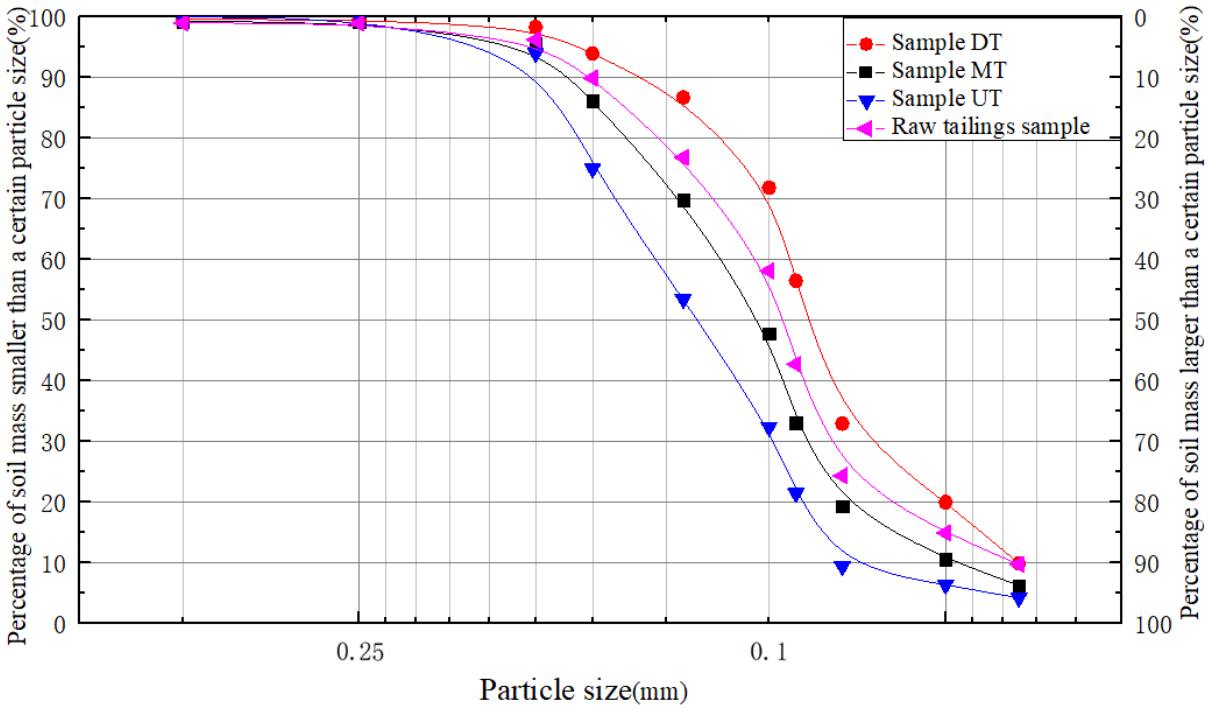
2.3 Results

The particle size distribution curve of each sample is plotted according to the results of Screening

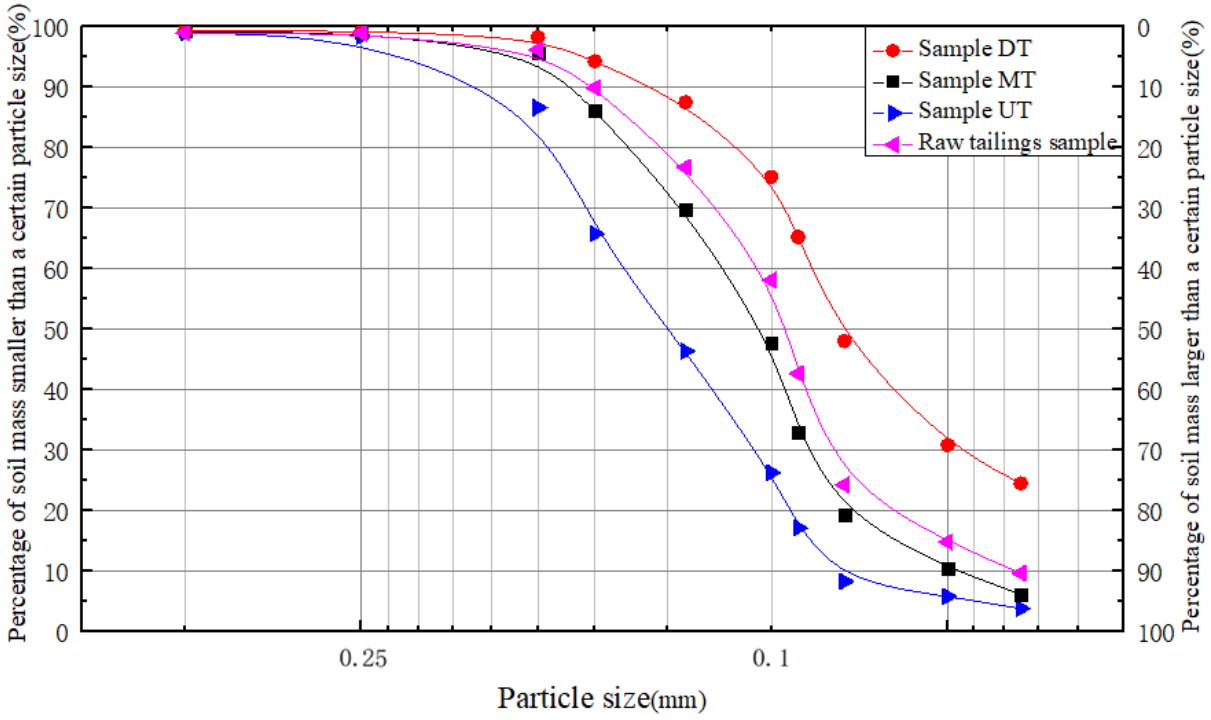
Test and Laser Particle Size Analysis, as shown in Fig.5.



(a) 1% slope



(b) 1.5% slope



(c) 2%slope

Fig. 5 Particle size distribution curves of sedimentary tailings samples at different slopes

As can be seen from Fig.5, the raw tailings were stratified along the slope of the Trapezoidal groove under the hydrodynamic force and gravitational force. The slope of the Trapezoidal groove has an important effect on the sedimentary characteristics of tailings, the greater the slope, the more obvious the stratification sedimentary of tailings. When the slope is 1%, the particle size distribution curves of downstream tailings(sample DT), midstream tailings(sample MT) and upstream tailings(sample UT) are shown in Fig.5(a). We can see that the average particle size of each sample has no significant change compared with that of the raw tailings, indicating that 1% slope is not conducive to the sedimentation of tailings due to low horizontal kinetic energy of tailings slurry. When the slope is 1.5%, we can see from Fig.5(b) that the sedimentary characteristics of tailings are more obvious than that of 1% slope, the average particle size of sample UT and sample MT increased by 16.4%, 11.4% respectively, the average particle size of sample DT decreased by 16.4% compared with that of the raw tailings. And the non-uniformity coefficient C_u of sample UT and sample MT increased due to amounts of fine-grained tailings being carried to the downstream. The amount of mid-grained tailings increased in the midstream and decreased significantly in the downstream of the model. When the slope is 2%, we can see from Fig.5(c) that the average particle size of sample UT and sample MT have more significant increase than that of 1.5% slope. The coarse-grained tailings and fine-grained tailings are more concentrated in the upstream and downstream of the model respectively, only 27.6% of the

upstream tailings have particles size smaller than 0.1mm, while more than 75.8% of the downstream tailings have particles size smaller than 0.1mm.

2.4 Discussion

The flow of tailing particles are affected by hydrodynamic force and gravitational force in Trapezoidal groove. As the flow velocity slows down, the hydrodynamic force decreases, and the coarse-grained tailings are deposited at first due to the greater gravity, resulting in the average particle size of upstream tailings is larger than that of downstream tailings in Trapezoidal groove. With the increase of Trapezoidal groove slope, the hydrodynamic force of tailing decreases slowly, which makes the fine-grained tailings migrate farther and has more obvious stratification sedimentary in Trapezoidal groove.

According to the literature[22], the probability of tailings sedimentary law can be expressed by Formula (4):

$$\lambda = \frac{vi}{W} \tag{4}$$

Where,

λ - judgment factor for tailings sedimentation

v - water velocity (m/s)

i - hydraulic gradient

W - sedimentary velocity of tailings (m/s)

When the λ value is greater than 1, the horizontal kinetic energy is greater than sedimentary energy, and the tailings slurry are hard to deposit; when the λ value is less than 1, the tailings slurry are easy to deposit. According to the particle size distribution curves of the hydraulic sedimentary test, the tailings with a diameter smaller than 0.075 mm are hard to deposit, mainly located in the downstream of the model. The tailings with a particle size of 0.075~0.15mm are mid-grained tailings primarily located in the middle of the model, its particle size distribution along the slope of the model is the most influenced by the hydrodynamic force. The tailings with a particle diameter larger than 0.15mm are quickly deposited on the upstream to form the tailings dam.

The average particle size distribution of sedimentary tailings along the slope of dry beach obeys the statistical law. According to the results of hydraulic sedimentary test, the average particle size D_{50} as a linear function of the dry beach length L at the dry beach slope of 1.5% can be expressed by the Formula (5).

$$D_{50} = 0.4394 - 6.51 \times 10^{-4} \times L \tag{5}$$

The relationship of average particle size D_{50} with the distance of sampling point from upstream L is shown in Fig.6.We can see that the test value of average particle size was consistent with that of on-site measured values, indating that the results of hydraulic sedimentary test can accurately reflect the sedimentary characteristics of dry beach tailings.

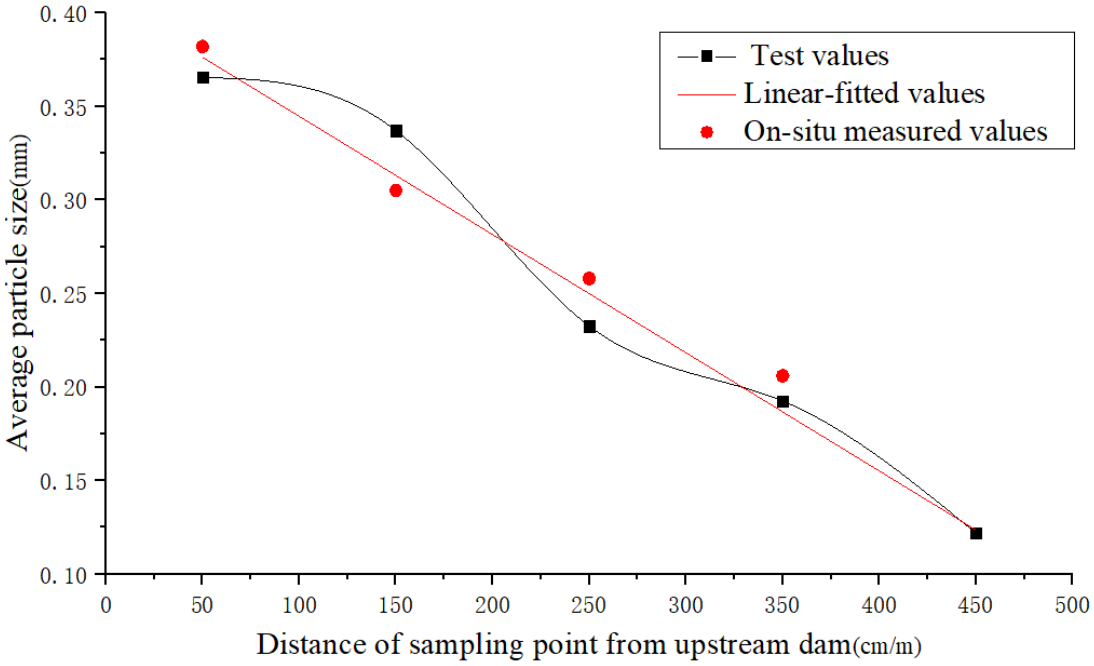


Fig. 6 The relationship between average particle size D_{50} and the distance of sampling point from upstream dam L

3.The effect of internal erosion on the physical and mechanical properties of tailings under heavy rainfall infiltration

3.1 Critical condition of internal erosion

In the porous medium, the fine-grained tailings are easy to be washed away under the seepage force, and the derivation process of the critical hydraulic gradient of internal erosion is derived as follows[23]:

The weight of saturated fine-grained tailings G' :

$$G' = (\gamma_s - \gamma_w) \cdot V \tag{6}$$

Where,

G' - Weight of fine-grained tailings (N)

γ_s - Bulk unit weight of fine tailings (N/ m^3)

γ_w - Bulk unit weight of water (N/ m^3)

V - Volume of fine tailings

The seepage force of fine-grained tailings is F :

$$F = i\gamma_w \cdot V \tag{7}$$

The initiation of fine-grained tailings should overcome the static friction force between the particles due to the cohesion of saturated tailings is 0:

$$f = G' \cdot tg\varphi \tag{8}$$

Where,

f - the static frictional resistance between the fine-grained tailings (N)

φ - internal friction angle of underwater fine-grained tailings (°)

The critical equilibrium condition for fine-grained tailings initiation is $F = f$,so the critical hydraulic gradient of internal erosion is i_{cr} : .

$$i_{cr} = \frac{G' \cdot tg\varphi}{\gamma_w \cdot V} \tag{9}$$

3.2 Experimental model

A sand columns model was established to investigate the effect of internal erosion on the physical and mechanical properties of tailings under unsteady seepage caused by heavy rainfall infiltration, as shown in Fig.7. The main body of the physical model consists of three sand columns (Column 1, Column 2 and Column 3) which are connected by flanges. And each sand column is made of polyvinyl chloride (PVC) with a maximum internal diameter 15 cm and a length of 30cm. The water pressure gauges are installed on the top of the model at a distance of 15 cm to measure the water head differences of each sand Column which can be controlled by adjusting the flow rate of the outlet flowmeter. A water tank with a maximum height of 3m connect to the model is used to simulate the raising saturation line of tailings dam under heavy rainfall infiltration.

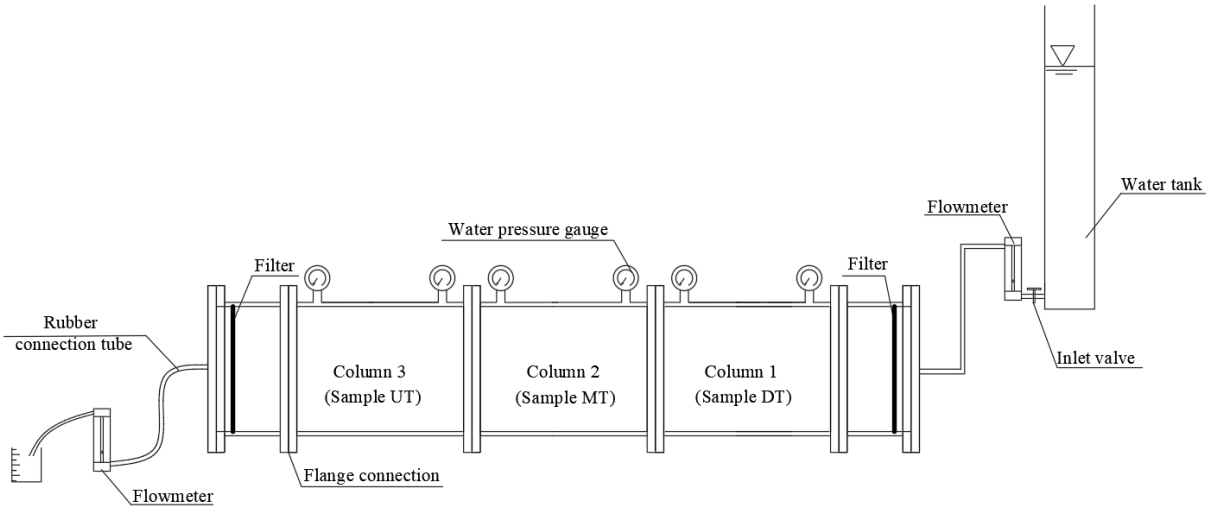


Fig. 7 Schematic diagram of unsteady seepage model

3.3 Experimental procedures

(1) Put the sedimentary tailings into the corresponding sand columns. The downstream tailings, midstream tailings and upstream tailings in hydraulic sedimentary test are filled into column 1, column 2 and column 3 respectively, to make the seepage direction of the physical model consistent with the actual seepage direction of the tailings dam.

(2) After installing the physical model, open the inlet valve to saturate the sand columns for 24h with water.

(3) Then adjust the outlet flowmeter to control the water head differences of each sand Column. When the value of each water pressure gauge is stable, the flow Q and water head differences of each sand column are recorded.

(4) Raise the water level of the water tank at a rate of 0.1m/h for 24 hours, which is consistent with the rising rate of saturation line of the tailings dam under heavy rainfall infiltration in a 50-years return period. The flow volume and the water head differences between the water pressure gauges are recorded each 1h.

3.4 Results

3.4.1 The effect of internal erosion on the hydraulic conductivity of tailings samples

The hydraulic conductivity K of each sand column is calculated according to flow Q and water head differences. The effect of internal erosion on the hydraulic conductivity of each sand column under unsteady seepage is shown in Fig. 8.

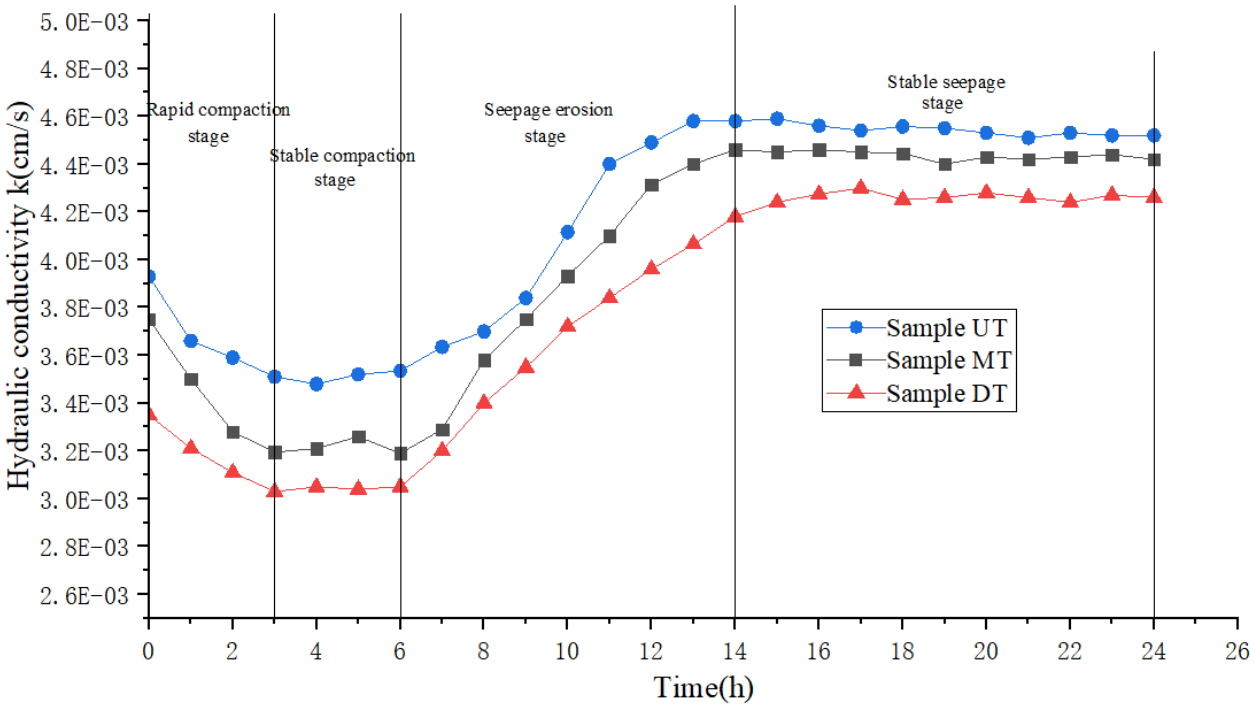


Fig. 8 Changes in hydraulic conductivity with time under unsteady seepage

As can be seen from Fig.8, initial hydraulic conductivity of each sand column is 3.35×10^{-3}cm/s(sample DT), 3.75×10^{-3}cm/s(sample MT) and $3.93\times\times10^{-3}$cm/s(sample UT). After 24 hours, the hydraulic conductivity of three sand columns increase to 4.26×10^{-3}cm/s, 4.42×10^{-3}cm/s, 4.53×10^{-3}cm/s, which increase by 27.2%,17.9%, and 15.3% respectively.

The change in hydraulic conductivity with time of sand columns can divide into four stages: rapid compaction stage, stable compaction stage, internal erosion stage and stable seepage stage. In stage 1 (1h–3h), there was the maximum decrease in hydraulic conductivity, the hydraulic conductivity of sample DT, sample MT and sample UT reduced by 9.5%, 14.9% and 10.7% respectively. The fine-grained tailings have a small range of migration due to the sudden increase of seepage force, which reduces the pore volume of downstream tailings and the hydraulic conductivity.In stage 2 (3h–6h), the hydraulic conductivity of each sand column tends to be stable due to the migration of fine-grained tailings and the increase of water head contributes to the balance of the hydraulic conductivity.In stage 3(6h–14h), there was the maximum increase in hydraulic conductivity, the hydraulic conductivity of sample DT, sample MT and sample UT increased by 37.1%, 39.8% and 29.7% respectively. In stage 4(14h–24h),the hydraulic conductivity of tailings samples remains constant regardless of the increase of water head, the tailings achieve a new stable state of hydraulic conductivity due to the particles of tailings were reorganized under the seepage force.

3.4.2 The effect of internal erosion on the shear strength of tailings samples

The tailings samples have been taken from each sand column in-situ for Direct Shear Test[24] after internal erosion test. The control shear rate was 0.8 mm/min. The shear strength and internal friction angle of each tailings sample before and after internal erosion are shown in Table 5.

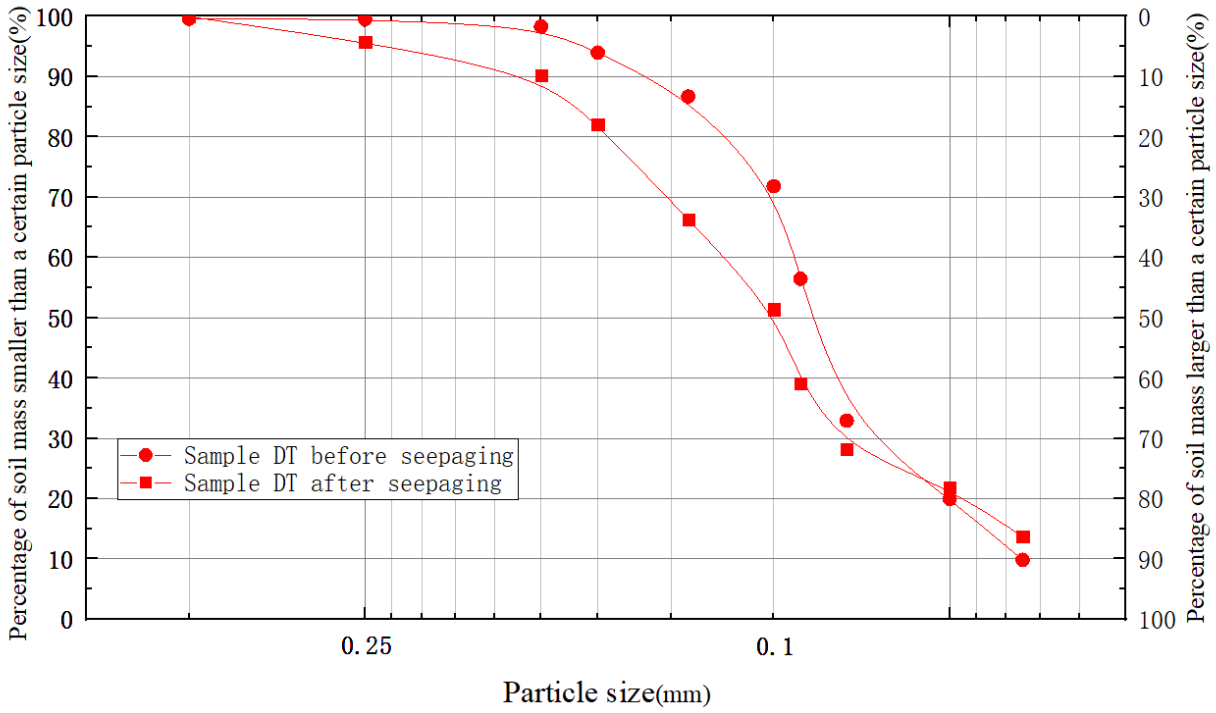
Table 5 The shear strength of tailings samples before and after internal erosion

Time	Tailings samples	Reduction rate of shear strength (%)	Internal friction angle (°)
Before internal erosion	Sample DT		35.14
	Sample MT		36.69
	Sample UT		38.70
After internal erosion	Sample DT	20.9	30.21
	Sample MT	15.1	32.94
	Sample UT	12.4	35.48

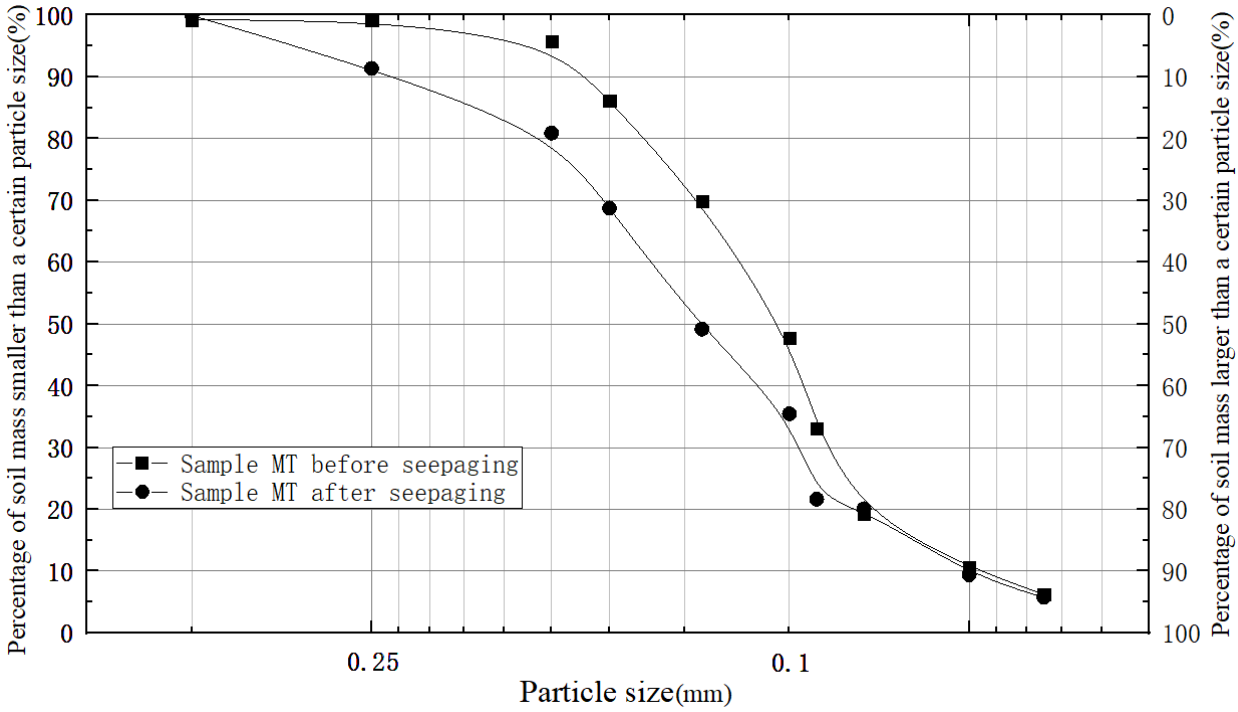
As can be seen from Table 5, the shear strength and internal friction angle of the tailings samples decreased after internal erosion, the shear strength of sample DT(Column 1), sample MT(Column 2) and sample UT(Column 3) decreased by 20.9 %, 15.1% and 12.4% respectively under 100 kPa normal press. The internal friction angle of sample DT, sample MT and sample UT decreased 14.0%, 10.2% and 8.3% respectively.

3.4.3 The effect of internal erosion on the particle size distribution curves of tailings samples

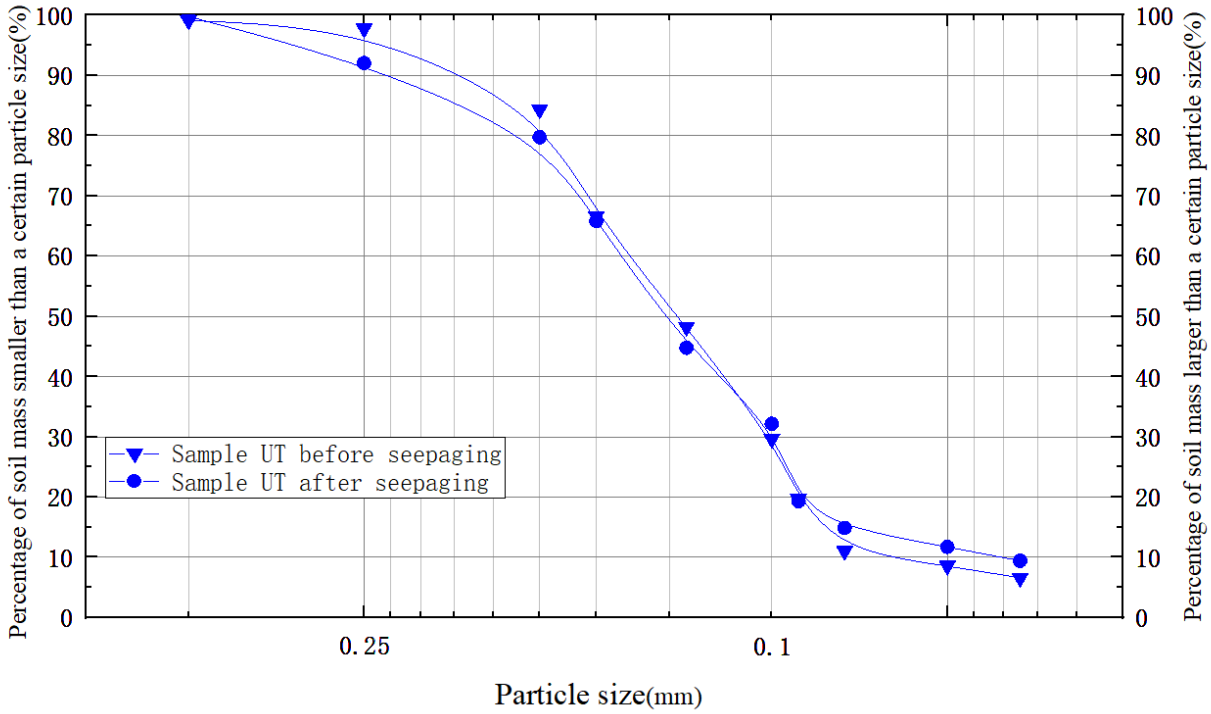
To further analyze the effect of internal erosion on the physical properties of the tailings samples, the tailings samples after internal erosion were taken for Screening Test. And the comparison of particle-size distribution curves of tailings samples before and after internal erosion test is shown in Fig. 9.



(a) Sample DT



(b) Sample MT



(c) Sample UT

Fig. 9 Comparison of Particle-size distribution curves of tailings samples before and after internal erosion

As can be seen from Fig.9, the average particle size of sample DT(Column 1), sample MT(Column 2) and sample UT(Column 3)increased by 6.4%, 12.0% and 2.4% respectively due to the migration of the fine-grained tailings along the seepage direction. About 20% tailings with particle size smaller than 0.075mm, and 10% tailings with the size of 0.075~0.1mm migrated to the downstream in the sample DT according to Fig.9(a). The change of average particle size of each tailings sample is not obvious; however, the mass of tailings with the particle size below 0.1 mm increase by about 4% in sample UT according to Fig.9(c).

3.5 Discussion

It can be seen from the internal corrosion test that the permeability of tailings has changed significantly under unsteady seepage caused by heavy rainfall infiltration. When the continuously rising water head gradient reaches the critical head gradient of tailings, lots of fine-grained tailings are washed away to the downstream, resulting in internal erosion and changing the skeleton structure of tailings. The critical hydraulic gradients of sample DT, sample MT and sample UT are calculated according to formula (9), which are 0.32, 0.36, 0.41 respectively.

The result of Direct Shear Test showed that internal erosion has the greatest influence on the shear strength and internal friction angle of fine-grained tailings compared to the coarse-grained tailings. The main reason for this phenomenon is the large-scale migration of fine particles in the upstream tailings, which leads to the change of particle size distribution of tailings. This conclusion is also

confirmed in Fig. 9.

The upstream tailings dam is more susceptible to internal erosion under unsteady seepage caused by heavy rainfall infiltration. The fine-grained tailings will be carried out of the tailings dam by the water, which is consistent with the actual observations. If this phenomenon is not seriously concerned, the safety of tailings dam will be affected over time.

4.Conclusions

Based on the above analysis and discussion, the following conclusions can be drawn:

(1) The average particle size D_{50} of sedimentary tailings decreases along the slope of dry beach. The slope of beach slope has an important effect on the sedimentary characteristics of tailings, the greater the slope, the more obvious the stratification sedimentary of tailings.

(2)The average particle size distribution along the groove slope in the hydraulic sedimentary test was consistent with that of on-site measured values, indicating that the test results can accurately reflect the sedimentary characteristics of dry beach tailings.

(3)The critical hydraulic gradient of sample DT, sample MT and sample UT are 0.32, 0.36, 0.41 respectively. When the hydraulic gradient of each tailing sample exceeds the critical value, the migration of the fine-grained tailings will result in internal erosion.

(4)The migration of fine-grained tailings caused by internal erosion increases the tailings' permeability and reduces the tailings' shear strength. After internal erosion, the hydraulic conductivity of sample DT, sample MT and sample UT increase by 27.2%, 17.9%, and 15.3% respectively, and the shear strength of sample DT, sample MT and sample UT decreased by 20.9 %, 15.1% and 12.4% respectively.

(5)The average particle size of sample DT, sample MT and sample UT increased by 6.4%, 12.0% and 2.4% respectively due to the migration of the fine-grained tailings along the seepage direction. More than 20% fine-grained tailings in the sample DT was migrated to the downstream.

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